

Ripley St Thomas A-Level Maths

Bridging Provision

## Introduction

In order to prepare for taking A-level maths next year, you need to ensure you are fluent in all aspect of GCSE, particularly algebra and those included in this booklet, and can approach problems with a confident, logical mindset.

You are expected to use this booklet to fill gaps in your knowledge, build confidence and ensure you start Alevel mathematics fully prepared. The knowledge and skills you find here, are essential for success in A-Level Mathematics.

The last 15 pages of this booklet are your first transition piece. This is compulsory and must be handed in during your first A-level mathematics lesson.

Success in A-Level Mathematics relies on an excellent attitude to learning and commitment to your studies. If you are struggling with any of the content in this booklet, you must use the video links included to brush up on these key skills. The videos stated are accessible on www.hegartymaths.com (if you have access to this through your current school) OR www.corbettmaths.com (for everyone).

## PLEASE NOTE HEGARTY MATHS CEASES TO EXIST ON $31^{\text {ST }}$ AUGUST. DO NOT LEAVE THIS DOCUMENT UNTIL THE DAY BEFORE YOU START SCHOOL.

## Additional resources to help you prepare.

As mentioned above it is important that you start Year 12 with an excellent attitude and be prepared to go above what is necessarily set as independent learning tasks. There are plenty of resources available online, please below for a few extra ideas to help you prepare for A-Level Maths.

1. Bridging the Gap - An A-Level maths tutor who produces videos and online resources. This page gives you the basics and videos with a A-Level spin. We do not recommend paying $£ 95$ per hour for the 1-1 tuition.


## Click or scan the QR Code

2. AMSP Transition to A-Level Essential Skills - AMSP produce amazing resources and these were designed for students to complete independently and will develop fluency in the fundamental techniques and the key mathematical concepts that underpin A level Mathematics.


## Click or scan the QR Code

3. Sparx Maths Transition Booklet - If your school uses SPARX then you can use the codes in the transition booklet. Otherwise this is just additional maths practice linked to the beginnings of A-Level.

4. OCRs Bridging the gap - Produced by OCR (an exam board) this is a bit more old school textbook style with examples and exercises. These have some tricky questions which will test your abilities well.

5. TL Maths - This person produces very good videos for A-Level maths and he has made a series of bridging videos to help with the transition.

Click or scan the QR Code

## Bridging Unit Content

Complete the 'RAG' table and use this as a starting point to direct your independent study. You can then revisit this and update your self-assessment as you grow in confidence.

|  | (1) | $\because$ | - |
| :---: | :---: | :---: | :---: |
| Quadratics |  |  |  |
| Factorise a quadratic expression where $\mathrm{a}=1$ |  |  |  |
| Factorise a 'DOTS' type quadratic expression |  |  |  |
| Factorise a quadratic expression where $\mathrm{a} \neq 1$ |  |  |  |
| Solve a quadratic equation by factorising |  |  |  |
| Write a quadratic expression in completed square form |  |  |  |
| Solve a quadratic equation by completing the square |  |  |  |
| Quadratic Graphs |  |  |  |
| Complete a table of values and plot a quadratic graph |  |  |  |
| Sketch a quadratic graph given its equation by: |  |  |  |
| - Finding the $x$-intercept(s) (if any) |  |  |  |
| - Finding the $y$-intercept |  |  |  |
| - Finding the coordinates of the vertex by writing in completed square form |  |  |  |
| Write down the equation of a quadratic given the graph |  |  |  |
| Linear Graphs |  |  |  |
| Write the equation for/draw a straight line using the gradient and intercept |  |  |  |
| Find the gradient and $y$-intercept of a line by rearranging its equation |  |  |  |
| Find the equation of a line using gradient and coordinates |  |  |  |
| Find the equation of a perpendicular line |  |  |  |
| Surds and Indices |  |  |  |
| Apply the Index Laws with numbers or algebra |  |  |  |
| Work with negative and fractional indices |  |  |  |
| Manipulate expressions containing surds (including simplifying surds, expanding brackets containing surds and rationalising a denominator) |  |  |  |
| Simultaneous Equations |  |  |  |
| Solve linear simultaneous equations by elimination |  |  |  |
| Solve linear simultaneous equations by substitution |  |  |  |
| Solve simultaneous equations where one is linear and one quadratic or a circle |  |  |  |
| Solve simultaneous equations graphically |  |  |  |
| Inequalities |  |  |  |
| Solve linear inequalities |  |  |  |
| Solve quadratic inequalities |  |  |  |
| Plot a region using inequalities on a graph |  |  |  |
| Trigonometry |  |  |  |
| Find sides and angles in triangles using SOHCAHTOA in 2d and 3d |  |  |  |
| Find angles, sides and areas in triangles using the Sine, Cosine and Area rules |  |  |  |
|  |  |  |  |

## GCSE to A Level Mathematics @ Ripley St Thomas



## Bridging Unit 1 - Quadratics

You need to be able to confidently:

- Factorise a quadratic expression where a = 1
- Factorise a 'DOTS' type quadratic expression
- Factorise a quadratic expression where $\mathrm{a} \neq 1$
- Solve a quadratic equation by factorising
- Write a quadratic expression in completed square form
- Solve a quadratic equation by completing the square


## 1. Factorise a quadratic expression where $\mathbf{a}=1$

## 户口 hegartymaths

Watch clip number \#223
Or Corbett Maths \#118

## Practice Exercise 1.1

Complete these questions on file paper.
Factorise these expressions:
1.
(a) $x^{2}+7 x+12$
(b) $x^{2}+6 x+8$
(c) $x^{2}+5 x+6$
(d) $x^{2}+8 x+7$
(e) $x^{2}+4 x+4$
(f) $x^{2}+8 x+15$
(g) $x^{2}+6 x+9$
(h) $\mathrm{x}^{2}+11 \mathrm{x}+28$
2.
(a) $\mathrm{x}^{2}+\mathrm{x}-12$
(b) $x^{2}+5 x-6$
(c) $x^{2}+3 x-10$
(d) $x^{2}+3 x-4$
(e) $x^{2}+2 x-48$
(f) $x^{2}+4 x-32$
(g) $x^{2}+2 x-35$
(h) $x^{2}+8 x-33$
3.
(a) $x^{2}-3 x-10$
(b) $\mathrm{x}^{2}-\mathrm{x}-20$
(c) $x^{2}-6 x-27$
(d) $x^{2}-2 x-3$
(e) $\mathrm{x}^{2}-\mathrm{x}-12$
(f) $x^{2}-4 x-12$
(g) $x^{2}-4 x-21$
(h) $x^{2}-6 x-55$
4.
(a) $x^{2}-6 x+9$
(b) $x^{2}-9 x+20$
(c) $x^{2}-9 x+14$
(d) $x^{2}-13 x+22$
(e) $\mathrm{x}^{2}-9 \mathrm{x}+8$
(f) $x^{2}-12 x+32$
(g) $x^{2}-15 x+36$
(h) $x^{2}-14 x+48$
5.
(a) $\mathrm{x}^{2}-9 \mathrm{x}+8$
(b) $x^{2}+24 x+23$
(c) $x^{2}-5 x-14$
(d) $x^{2}-7 x+12$
(e) $x^{2}+12 x+36$
(f) $x^{2}-2 x-63$
(g) $x^{2}+14 x+24$
(h) $x^{2}+17 x+60$

Mark your work.

## 2. Factorise a 'DOTS' quadratic expression

## 良hegartymaths <br> Watch clip number \#224 <br> Or Corbett Maths \#120

## Practice Exercise 1.2

Complete these questions on file paper.
Factorise these expressions:

1. (a) $x^{2}-25$
(b) $y^{2}-49$
(c) $\mathrm{w}^{2}-100$
(d) $x^{2}-4$
(e) $c^{2}-64$
(f) $x^{2}-1$
(g) $x^{2}-900$
(h) $y^{2}-9$
(i) $16-\mathrm{x}^{2}$
(j) $1-y^{2}$
(k) $81-x^{2}$
(l) $144-\mathrm{h}^{2}$
(m) $x^{2}-y^{2}$
(n) $a^{2}-c^{2}$
(o) $9 x^{2}-25$
(p) $4 y^{2}-1$
2. 

(a) $\mathrm{x}^{4}-1$
(b) $y^{4}-16$
(c) $\mathrm{a}^{4}-25$
(d) $x^{4}-y^{4}$
(e) $h^{2}-p^{4}$
(f) $16 \mathrm{x}^{4}-49$
(g) $y^{6}-36$
(h) $x^{6}-64$
(i) $81 \mathrm{p}^{4}-\mathrm{x}^{6}$
(j) $144 \mathrm{x}^{8}-1$

Mark your work.

## 3. Factorise a quadratic where $\mathbf{a} \neq 1$

## 良hegartymaths

Watch clip number \#225
Or Corbett Maths \#119

## Practice Exercise 1.3

Complete these questions on file paper.
Factorise these expressions:
1.
(a) $2 x^{2}+7 x+5$
(b) $2 x^{2}+11 x+15$
(c) $2 x^{2}+9 x+10$
(d) $3 x^{2}+13 x+4$
(e) $3 x^{2}+4 x+1$
(f) $3 x^{2}+8 x+4$
2.
(a) $3 x^{2}+x-4$
(b) $7 x^{2}+20 x-3$
(c) $2 x^{2}-13 x+15$
(d) $3 x^{2}-17 x+10$
(e) $3 x^{2}-16 x-12$
(f) $3 x^{2}-x-4$
3.
(a) $6 x^{2}+13 x+6$
(b) $9 x^{2}+9 x+2$
(c) $6 x^{2}+13 x+2$
(d) $8 x^{2}+41 x+5$
(e) $9 x^{2}+6 x+1$
(f) $8 x^{2}+26 x+15$
4.
(a) $9 x^{2}-12 x-5$
(b) $4 x^{2}-4 x-3$
(c) $4 x^{2}-11 x+6$
(d) $6 x^{2}-7 x+2$
(e) $10 x^{2}-91 x+9$
(f) $4 x^{2}+25 x-56$

Mark your work.

## 4. Solve a quadratic equation by factorising

## ¢ . hegartymaths

Watch clip number \#230
Or Corbett Maths \#266

## Practice Exercise 1.4

Complete these questions on file paper.
Solve these equations by factorising:
1.
(a) $\mathrm{x}^{2}+6 \mathrm{x}+8=0$
(b) $x^{2}+7 x+12=0$
(c) $y^{2}+7 y+10=0$
(d) $y^{2}+3 y-4=0$
(e) $x^{2}-2 x-8=0$
(f) $\mathrm{m}^{2}-7 \mathrm{~m}+12=0$
(g) $y^{2}-10 y+25=0$
(h) $y^{2}-4 y-45=0$
(i) $\mathrm{x}^{2}-\mathrm{x}-56=0$
2.
(a) $x^{2}-9=0$
(b) $\mathrm{y}^{2}-100=0$
(c) $\mathrm{w}^{2}-1=0$
(d) $\mathrm{k}^{2}-144=0$
(e) $x^{2}-64=0$
(f) $\mathrm{c}^{2}-0.25=0$
3.
(a) $x^{2}+2 x=-1$
(b) $\mathrm{y}^{2}+8 \mathrm{y}+10=3$
(c) $\mathrm{x}^{2}=7 \mathrm{x}-12$
(d) $y^{2}+6 y+15=3-7 y$
(e) $\mathrm{x}^{2}-\mathrm{x}-8=2 \mathrm{x}+2$
(f) $2 x^{2}-14 x+49=x^{2}$

Mark your work.

## 5. Write a quadratic in completed square form

## 穴hegartymaths

Watch clip number \#235-237
Or Corbett Maths \#10

## Practice Exercise 1.5

Complete these questions on file paper.
Write these expressions in completed square form:

1. (a) $x^{2}+8 x+1$
(b) $x^{2}+10 x+3$
(c) $x^{2}+2 x-1$
(d) $x^{2}-6 x-10$
(e) $x^{2}-4 x-13$
(f) $x^{2}-12 x+3$
(g) $x^{2}+14 x+3$
(h) $x^{2}-2 x-15$
(i) $\mathrm{x}^{2}+4 \mathrm{x}-11$
(j) $x^{2}+x-8$
(k) $x^{2}+3 x+1$
(l) $x^{2}-7 x-2$
2. 

(a) $2 x^{2}+8 x+2$
(b) $2 x^{2}+12 x-3$
(c) $3 x^{2}-12 x+2$
(d) $4 x^{2}+12 x-5$
(e) $2 x^{2}-3 x-5$
(f) $5 \mathrm{x}^{2}-20 \mathrm{x}+30$

Mark your work.

## 6. Solve a quadratic equation by completing the square

## 关 hegartymaths

Watch clip number \#238-239
Or Corbett Maths \#267a

## Practice Exercise 1.6

Complete these questions on file paper.
Solve these equations by completing the square:
1.
(a) $\mathrm{x}^{2}+6 \mathrm{x}+8=0$
(b) $\mathrm{x}^{2}+10 \mathrm{x}+24=0$
(c) $\mathrm{x}^{2}+14 \mathrm{x}+40=0$
(d) $x^{2}-4 x-45=0$
(e) $x^{2}-12 x+35=0$
(f) $x^{2}-2 x-3=0$
2.
(a) $\mathrm{x}^{2}+5 \mathrm{x}+4=0$
(b) $\mathrm{x}^{2}-3 \mathrm{x}-18=0$
(c) $\mathrm{x}^{2}+\mathrm{x}-12=0$
(d) $x^{2}-7 x+12=0$
(e) $\mathrm{x}^{2}-11 \mathrm{x}+24=0$
(f) $x^{2}-7 x-30=0$
3. Write your answers in surd form where appropriate:
(a) $\mathrm{x}^{2}+4 \mathrm{x}-3=0$
(b) $\mathrm{x}^{2}+6 \mathrm{x}-10=0$
(c) $x^{2}-2 x-5=0$
(d) $x^{2}-10 x+1=0$
(e) $\mathrm{x}^{2}+8 \mathrm{x}+3=0$
(f) $x^{2}-8 x-22=0$
4.
(a) $5 x^{2}+30 x-10=0$
(b) $2 x^{2}+7 x+3=0$
(c) $3 x^{2}+12 x-2=0$
(d) $2 x^{2}-3 x-7=0$
(e) $5 x^{2}+2 x-8=0$
(f) $10 x^{2}-2 x-1=0$

Mark your work.

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## Bridging Unit 2 - Quadratic Graphs

You need to be able to confidently:

- Complete a table of values and plot a quadratic graph
- Sketch a quadratic graph given its equation by
- Finding the $x$-intercept(s) (if any)
- Finding the $y$-intercept
- Finding the coordinates of the vertex by writing in completed square form
- Write down the equation of a quadratic given the graph


## 1. Complete a table of values and plot a quadratic graph

## $\stackrel{\circ}{\text { • }}$ hegartymaths

Watch clip number \#251

Or Corbett Maths \#264

## Practice Exercise 2.1

Print out the next page and answer the questions on it.

- If you use a calculator to work out the values, remember that when $x$ is negative you must put brackets around it when you square it, i.e. $(-3)^{2}$.
- Make sure that you plot and draw the graphs in pencil.
- If your graph is not a smooth $U$ or $\cap$ shape then at least one of your values must be incorrect or you have plotted something incorrectly, so look for your mistake and correct it.
- Each graph should be symmetrical, but not necessarily in the $y$-axis (and remember that you are only plotting a small section of it).

1. $y=x^{2}-4$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ |  |  |  |  |  |  |  |

2. $y=x^{2}+2 x$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ |  |  |  |  |  |  |  |



3. $y=5 x-x^{2}$
4. $y=x^{2}+4 x+7$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ |  |  |  |  |  |  |  |



Mark your work.

## 2. Sketch a quadratic graph given its equation

This previous section was about plotting an accurate quadratic curve on numbered coordinate axes. What we are talking about here is sketching the correct shape of a quadratic graph, without scales on the axes but labelling the significant points with their coordinates (the intercepts and turning point).

## 穴 hegartymaths <br> Watch clip number \#257 <br> Or Corbett Maths \#265

## Practice Exercise 2.2

Complete these questions on squared paper.
Draw your graphs in pencil, and axes with a ruler.

For each question show that you have:
a. Decided whether the graph is U-shaped (if the coefficient of $x^{2}$ is positive) or $n$-shaped (if the coefficient of $x^{2}$ is negative).
b. Found the $x$-intercept(s) by setting $y=0$ and solving the equation (by any of the methods from Unit 1).
c. Found the $y$-intercept by setting $x=0$.
d. Found the coordinates of the vertex by writing the equation in completed square form.

1. Sketch the graph of $y=x^{2}+10 x+9$
2. Sketch the graph of $y=x^{2}+6 x+8$
3. Sketch the graph of $y=x^{2}-2 x-3$
4. Sketch the graph of $y=-x^{2}-2 x+8$

Mark your work.

## 3. Write down the equation of a quadratic given the graph

## 穴 hegartymaths

If necessary watch clip number \#257 again.
Or Corbett Maths \#265

## Practice Exercise 2.3

Complete these questions on file paper.
Write down the equations of the graphs shown.

You are now working backwards from what you did before.

- If you know the coordinates of the vertex you can write the equation in completed square form.
- If you know the $x$-intercept(s) you can write the equation in factorised form.

In either case check your answer by expanding and simplifying, then checking that the $y$-intercept is correct.
1.

2.

3.

4.


Mark your work.

## GCSE to A Level Mathematics @ Ripley St Thomas



## Bridging Unit 3 - Linear Graphs

You need to be able to confidently:

- Write the equation for/draw a straight line using the gradient and intercept
- Find the gradient and $y$-intercept of a line by rearranging its equation
- Find the equation of a line using gradient and coordinates
- Find the equation of a perpendicular line


## 1. Write the equation for/draw a straight line using the gradient and intercept

This unit assumes that you can draw a straight line graph by filling in a table of values and plotting points.

## $\stackrel{\circ}{\text {, hegartymaths }}$

Watch clip number \#207-209
Or Corbett Maths \#187

## Practice Exercise 3.1

Complete these questions on squared paper.

1. Write down the gradient and $y$-intercept of the line with equation:
a) $y=7 x-8$
b) $y=2 x+9$
c) $y=0.5 x$
2. Write down the equation of the line with:
a) Gradient 5 and $y$-intercept -2
b) Gradient 10 and $y$-intercept 7
c) Gradient -3 and $y$-intercept 1
3. On squared paper, draw the graphs from questions 1 and 2.

Do not use a table of values; use the gradient and $y$-intercept.
4. Write down the equation of these graphs by identifying the gradient and $y$-intercept:
a)

b)

c)

d)


Mark your work.

## 2．Find the gradient and $y$－intercept of a line by rearranging its equation

## 户大 hegartymaths <br> Watch clip number \＃210 <br> Or Corbett Maths \＃191

## Practice Exercise 3.2

Complete these questions on file paper．

For each question：
a）Use the balance method（showing all your working）to rearrange these equations into the form $y=m x+c$
b）Identify the gradient and $y$－intercept．
1．$x+y=13$
2．$\frac{y}{2}=2 x+3$
3． $2 x-y=-7$
4． $4 x+2 y=5$
5．$x=20-4 y$
6． $6 x=2 y+3$
7． $6 x=\frac{y}{3}+3$
8． $6 x=7(y-1)$
9． $6(x-2)=5 y$
10． $6 x-5 y=4$

Mark your work．

## 3．Find the equation of a line using gradient and coordinates

## 康 hegartymaths <br> Watch clip number \＃212 <br> Or Corbett Maths \＃194

## Practice Exercise 3.3

Complete these questions on file paper．
Write down the equation of the graph which：

1．Has gradient 3 and goes through（1，4）．
2．Has gradient 7 and goes through（ $-2,7$ ）．
3．Has gradient -2 and goes through $(2,4)$ ．4．Has gradient -10 and goes through $(-3,5)$ ．

5．Goes through $(0,4)$ and $(2,10)$ ．
6．Goes through $(2,10)$ and $(4,14)$ ．
7. Goes through $(-1,-4)$ and $(7,12)$. 8. Goes through $(3,-7)$ and $(11,-3)$.
9. Is parallel to the line $y=4 x+2$ and goes through the point $(4,5)$.
10. Is parallel to the line $x+y=6$ and goes through the point ( $3,-7$ ).
11. Is parallel to the line $x-y=5$ and goes through the point $(3,10)$.
12. Is parallel to the line $x-2 y=16$ and goes through the point $(-4,5)$.

Mark your work.

## 4. Find the equation of a perpendicular line

## 实 hegartymaths

Watch clip number \#216
Or Corbett Maths \#197

## Practice Exercise 3.4

Complete these questions on file paper.

1. Find the equation of the line which is perpendicular to the line $y=2 x-8$ and goes through the point $(0,4)$.
2. Find the equation of the line which is perpendicular to the line $y=-3 x+13$ and goes through the point $(1,2)$.
3. Find the equation of the line which is perpendicular to the line $y=\frac{1}{2} x$ and goes through the point $(5,8)$.
4. Find the equation of the line which is perpendicular to the line $y=\frac{1}{8} x-3$ and goes through the point ( $-1,4$ ).
5. Find the equation of the line which is perpendicular to the line $y=-\frac{2}{3} x+23$ and goes through the point $(3,-5)$.

Mark your work.

## GCSE to A Level Mathematics @ Ripley St Thomas



## Bridging Unit 4 - Indices and Surds

You need to be able to confidently:

- Apply the Index Laws with numbers or algebra
- Work with negative and fractional indices
- Manipulate expressions containing surds (including simplifying surds, expanding brackets containing surds and rationalising a denominator)


## 1. Apply the Index Laws with numbers or algebra

## \& hegartymaths

Watch clip number \#110
Or Corbett Maths \#174

## Practice Exercise 4.1a

Complete these questions on file paper. Do not use a calculator.
1 Write as a power of 2
a $2^{4} \times 2^{5}$
b $2^{3} \times 2^{4}$
c $2^{2} \times 2^{6}$
d $2^{4} \times 2^{3}$
e $2^{4} \times 2^{6}$

2 Write as a power of 3
a $3^{4} \div 3^{2}$
b $3^{5} \div 3^{2}$
c $3^{4} \div 3$
d $3^{6} \div 3^{2}$
e $3^{10} \div 3^{4}$

3 Write as a power of a single number
a $4^{4} \div 4^{2}$
b $5^{7} \div 5^{2}$
c $3^{4} \times 3^{2}$
d $6^{4} \times 6^{3}$
e $10^{4} \div 10^{2}$

4 Find the value of $n$
a $3^{n} \div 3^{2}=3^{3}$
b $8^{5} \div 8^{n}=8^{2}$
c $2^{5} \times 2^{n}=2^{10}$
d $3^{n} \times 3^{5}=3^{9}$
e $2^{6} \times 2^{3}=2^{n}$

5 Work out
a $3^{4} \div 3^{2}$
b $4^{5} \div 4^{3}$
c $2^{5} \div 2^{2}$
d $10^{4} \times 10^{2}$
e $6^{5} \div 6^{5}$

6 Write as a power of 3
a $\frac{3^{3} \times 3^{5}}{3^{4}}$
b $\left(3^{3}\right)^{2}$
c $\frac{3 \times 3^{7}}{3^{4}}$
d $\frac{3^{9}}{3^{4} \times 3^{3}}$
e $\frac{3^{2} \times 3^{10}}{3^{2} \times 3^{5}}$

7 Write as a power of a single number
a $\frac{2^{3} \times 2^{4}}{2^{5}}$
b $\frac{3^{4} \times 3^{3}}{3^{4}}$
c $\frac{5^{3} \times 5^{5}}{5^{6}}$
d $\frac{10^{8} \times 10^{3}}{10^{7}}$
e $\frac{4^{5} \times 4}{4^{2}}$

8 Work out
a $\frac{5^{5}}{5^{2} \times 5^{2}}$
b $\frac{3^{4}}{3^{2} \times 3^{2}}$
c $\frac{4^{7}}{4^{2} \times 4^{3}}$
d $\frac{2^{3} \times 2^{4}}{2^{4} \times 2^{2}}$
e $\frac{3 \times 3^{7}}{3^{4} \times 3^{2}}$

9 Work out the value of $n$ in the following.
a $40=5 \times 2^{n}$
b $32=2^{n}$
c $50=5^{n} \times 2$
d $48=3 \times 2^{n}$
e $54=2 \times 3^{n}$

Mark your work.

## Practice Exercise 4.1b

Complete these questions on file paper.
1 Simplify
a $x^{3} \times x^{2}$
b $y^{5} \times y^{3}$
c $n \times n^{6}$
d $q^{7} \times q$
e $x^{5} \div x^{3}$
f $y^{7} \div y^{3}$
g $p^{5} \div p^{4}$
h $q^{7} \div q$
i $y \times y^{4} \times y^{3}$
j $q^{4} \times q \div q^{3}$

2 Simplify
a $3 x^{2} \times x^{5}$
b $4 p \times 2 p^{4}$
c $4 p \times 5 p$
d $2 \times 2 r^{8} \times 4 r$
e $6 y^{6} \div 2 y^{3}$
f $12 q^{2} \div 6 q$
g $8 x^{9} \div 2 x^{8}$
h $4 q \div 2 q$
i $2 y^{2} \times 3 y^{3} \times y^{3}$
j $6 q \times 5 q^{4} \div 2 q^{5}$

3 Simplify
a i $x^{2} \times x$
ii $x^{5} \div x^{2}$
iii $\left(x^{2} \times x\right)+\left(x^{5} \div x^{2}\right)$
b $\left(8 y^{6} \div 2 y^{2}\right)-\left(2 y^{2} \times y^{2}\right)$

4 Simplify
a $3 a^{4} \times a^{3} b^{2}$
b $2 a b^{4} \times 4 a^{3} b$
c $5 p^{4} q^{3} \times 2 q^{3} p^{2}$
d $18 x^{8} y^{6} \div 6 x^{3} y^{2}$
e $12 a^{3} b^{5} \div 3 a^{3} b$
f $20 p^{4} q \div 2 p^{3} q^{2}$

5 Find the value of
a $4 x^{0}$
b $(x y)^{0}$

6 Write as a power of $x$
a $\frac{1}{x^{4}}$
b $\frac{1}{x}$
c $\frac{1}{x^{4} \times x^{3}}$
d $\frac{1}{x^{4} \div x}$
e $\frac{1}{x^{5} \div x^{7}}$

7 Simplify
a $\left(x^{5}\right)^{3}$
b $\left(2 y^{2}\right)^{4}$
c $\left(a^{2} b^{4}\right)^{5}$
d $\left(3 a^{3} b\right)^{3}$
e $\left(x^{2}\right)^{-1}$
f $\left(4 y^{-2}\right)^{2}$
g $\left(a^{-4}\right)^{-3}$
h $\left(-2 b^{-4}\right)^{-2} \div b^{2}$

8 Simplify
a $\left(x^{2}\right)^{0}$
b $\left(y^{0}\right)^{4}$
c $\left(2 a^{3} b^{-2}\right)^{-3} \times\left(2 a^{-3} b\right)^{3}$

Mark your work.

## 2. Work with negative and fractional indices

## 穴hegartymeths

If necessary watch clip number \#110 again Or Corbett Maths \#173 \& \#175

## Practice Exercise 4.2a

## Complete these questions on file paper. Do not use a calculator.

1 Work out the value of the following.
a $2^{-1}$
b $3^{-2}$
c $5^{-1}$
d $10^{-3}$
e $2^{0}$
f $2.5^{-1}$
g $\left(\frac{1}{3}\right)^{-1}$
h $\left(\frac{2}{3}\right)^{-2}$

2 Simplify the following.
a $3^{2} \times 3^{-3}$
b $4^{-2} \times 4$
c $5^{4} \times 5^{-2}$
d $6^{2} \times 6^{-4}$
e $2^{2} \times 2^{-5}$

3 Simplify the following.
a $4^{-2} \div 4^{-1}$
b $3^{2} \div 3^{-1}$
c $2^{-2} \div 2^{-4}$
d $10^{-4} \div 10^{-3}$
e $5^{-3} \div 5^{-1}$

4 Simplify the following.
a $\frac{2^{4} \times 2^{2}}{2^{7}}$
b $\frac{3^{4} \times 3^{-2}}{3^{3}}$
c $\frac{5^{-2} \times 5^{2}}{5}$
d $\frac{4^{-3} \times 4^{3}}{4^{-2}}$
e $\frac{2^{-4} \times 2^{2}}{2^{-7}}$

5 Simplify the following.
a $\frac{2^{4}}{2^{7} \times 2^{-2}}$
b $\frac{3^{4} \times 3^{2}}{3 \times 3^{7}}$
c $\frac{5^{4} \times 5^{-2}}{5^{2} \times 5^{-1}}$
d $\frac{4^{4} \times 4^{-2}}{4^{-1}}$
$e \frac{2^{4} \times 2^{2}}{2^{7} \times 2^{-1}}$

6 Find the value of $n$ in each of the following.
a $2^{n}=\frac{2^{2}}{2^{5}}$
b $3 \times 3^{n}=\frac{3^{3}}{3^{5}}$
c $\frac{5^{n}}{5}=\frac{5^{2}}{5^{5}}$
d $4^{2} \times 4^{n}=\frac{4^{2}}{4^{6}}$

Mark your work.

## Practice Exercise 4.2b

## Complete these questions on file paper. Do not use a calculator.

1 Work out the value of
a $9^{\frac{1}{2}}$
b $25^{\frac{1}{2}}$
c $100^{\frac{1}{2}}$
d $4^{\frac{1}{2}}$
e $\left(\frac{1}{4}\right)^{\frac{1}{2}}$

2 Work out the value of
a $27^{\frac{1}{3}}$
b $1000^{\frac{1}{3}}$
c $-64^{\frac{1}{3}}$
d $125^{\frac{1}{3}}$
e $\left(\frac{1}{125}\right)^{\frac{1}{3}}$

3 Work out as a single fraction the value of
a $\left(\frac{1}{2}\right)^{4}$
b $\left(\frac{1}{3}\right)^{2}$
c $\left(\frac{2}{3}\right)^{2}$
d $\left(\frac{2}{5}\right)^{2}$
e $\left(\frac{3}{4}\right)^{3}$

4 Work out the value of
a $27^{\frac{2}{3}}$
b $1000^{\frac{2}{3}}$
c $64^{\frac{2}{3}}$
d $16^{\frac{3}{4}}$
e $25^{\frac{3}{2}}$

5 Work out as a single fraction the value of
a $25^{-\frac{1}{2}}$
b $9^{-\frac{1}{2}}$
c $27^{-\frac{1}{3}}$
d $8^{-\frac{2}{3}}$
e $64^{-\frac{3}{2}}$

6 Find the value of $n$.
a $\frac{1}{\sqrt{5}}=5^{n}$
b $(\sqrt{7})^{5}=7^{n}$
c $(\sqrt[3]{2})^{11}=2^{n}$

Mark your work.

## 3. Manipulate expressions containing surds

(including simplifying surds, expanding brackets containing surds and rationalising a denominator)

## 良 hegartymaths

Watch clip numbers \#115, \#117-119

Or Corbett Maths \#308 \& \#307

## Practice Exercise 4.3

Complete these questions on file paper.

1 Find the value of the integer $k$.
a $\sqrt{8}=k \sqrt{2}$
b $\sqrt{18}=k \sqrt{2}$
c $\sqrt{50}=k \sqrt{2}$
d $\sqrt{80}=k \sqrt{5}$
e $\sqrt{72}=k \sqrt{2}$

2 Expand these expressions. Write your answers in the form $a+b \sqrt{c}$ where $a, b$ and $c$ are integers.
a $\sqrt{3}(2+\sqrt{3})$
b $(\sqrt{3}+1)(2+\sqrt{3})$
c $(\sqrt{5}-1)(2+\sqrt{5})$
d $(\sqrt{7}+1)(2-2 \sqrt{7})$
e $(2-\sqrt{3})^{2}$

3 Rationalise the denominators.
a $\frac{1}{\sqrt{2}}$
b $\frac{1}{\sqrt{5}}$
c $\frac{2}{\sqrt{7}}$
d $\frac{3}{\sqrt{2}}$
e $\frac{5}{\sqrt{11}}$

4 Rationalise the denominators and simplify your answers.
a $\frac{2}{\sqrt{6}}$
b $\frac{3}{\sqrt{12}}$
c $\frac{5}{\sqrt{10}}$
d $\frac{2}{\sqrt{2}}$
e $\frac{10}{\sqrt{5}}$

5 Rationalise the denominators and give your answers in the form $a+b \sqrt{c}$ where $a, b$ and $c$ are integers.
a $\frac{2+\sqrt{2}}{\sqrt{2}}$
b $\frac{2-\sqrt{2}}{\sqrt{2}}$
c $\frac{10+\sqrt{5}}{\sqrt{5}}$
d $\frac{5-\sqrt{5}}{\sqrt{5}}$
e $\frac{14+\sqrt{7}}{\sqrt{7}}$

6 The lengths of the two shorter sides of a right-angled triangle are $\sqrt{7} \mathrm{~cm}$ and 3 cm . Find the length of the hypotenuse.

7 The length of the side of a square is $(1+\sqrt{2}) \mathrm{cm}$. Work out the area of the square. Give your answer in the form $(a+b \sqrt{2}) \mathrm{cm}^{2}$ where $a$ and $b$ are integers.

8 The length of a rectangle is $(3+\sqrt{5}) \mathrm{cm}$. The width of the rectangle is $(4-\sqrt{5}) \mathrm{cm}$.
Work out $\mathbf{a}$ the perimeter of the rectangle $\mathbf{b}$ the area of the rectangle.

Mark your work.

## GCSE to A Level Mathematics @ Ripley St Thomas



## Bridging Unit 5 - Simultaneous Equations

You need to be able to confidently:

- Solve linear simultaneous equations by elimination
- Solve linear simultaneous equations by substitution
- Solve simultaneous equations where one is linear and one quadratic or a circle
- Solve simultaneous equations graphically


## 1. Solve linear simultaneous equations by elimination

## 穴hegartymaths

Watch clip number \#192-193
Or Corbett Maths \#295

## Practice Exercise 5.1

Complete these questions on file paper.

1. (a) $6 x+y=18$
$4 x+y=14$
(b) $4 x+2 y=10$
$x+2 y=7$
(c) $\quad 9 x-4 y=19$
$4 x+4 y=20$
(d) $2 x+y=36$
$x-y=9$
(e) $\quad 6 x-3 y=12$
$4 x-3 y=2$
(f) $\quad 3 x-6 y=6$
$2 x-6 y=3$
2. 

(a) $3 x+2 y=23$
$2 x-y=6$
(b) $\quad \begin{aligned} & 3 x-3 y=9 \\ & 2 x+y=12\end{aligned}$
(c) $\quad 4 x+2 y=34$
$3 x+y=21$
(d) $9 x-4 y=59$
$2 x-y=12$
(e) $\quad \begin{aligned} & 2 x+8 y=43 \\ & x+3 y=18\end{aligned}$
(f) $6 x+3 y=45$
$2 x-2 y=12$
3.
(a) $2 x+2 y=14$
(b) $2 x+3 y=1$ $5 x-3 y=19$
$7 x+2 y=-22$
(c) $5 x+3 y=22$
$2 x+4 y=20$
(d) $5 x-6 y=28$
(e) $3 x+2 y=7$
(f) $3 x+3 y=-6$
$4 x-4 y=24$
$2 x+9 y=43$
$4 x-4 y=-24$

Mark your work.

## 2. Solve linear simultaneous equations by substitution

Watch clip number \#194.
hegartymaths
Or Corbett Maths \#296 \& \#298

## Practice Exercise 5.2

Complete these questions on file paper.
1.
(a) $\begin{aligned} y & =x+3 \\ y & =x^{2}+5 x-2\end{aligned}$
(b) $\begin{aligned} y & =x^{2}+x-14 \\ y & =x-5\end{aligned}$
(c) $\mathrm{y}=2 \mathrm{x}-1$
$y=x^{2}-2 x+2$
(d) $y=2 x^{2}+9 x+1$ $y=3 x+9$
(e) $\mathrm{y}=2 \mathrm{x}^{2}+\mathrm{x}+1$ $y=x^{2}-5 x-7$
(f) $y=-x^{2}+5 x+2$ $y=3 x^{2}-x-2$
2.
(a) $x+y=4$ $y=x^{2}+3 x-1$
(b) $x+y=7$ $x y=10$
(c) $\mathrm{x}^{2}+\mathrm{y}^{2}=13$ $x+y=5$
(d) $2 \mathrm{x}-\mathrm{y}+4=0$ $y=x^{2}+x-2$
(e) $\mathrm{x}^{2}+\mathrm{y}^{2}=29$
$7+\mathrm{x}+\mathrm{y}=0$
(f) $x y=-6$ $x+2 y=-4$
3.
(a) $\quad \begin{aligned} & 2 x+y=7 \\ & x^{2}-y^{2}=8\end{aligned}$
(b) $\mathrm{x}^{2}+\mathrm{y}^{2}=20$ $y=x+3$
(c) $\mathrm{y}=\mathrm{x}^{2}-9 \mathrm{x}-3$ $y=x$
(d) $2 \mathrm{x}^{2}+\mathrm{y}^{2}=10$ $2 x-y=5$
(e) $y=x^{2}+x-7$
$4 x+2 y+1=0$
(f) $\mathrm{y}=\mathrm{x}-2$ $2 x^{2}-x y=11$

Mark your work.
3. Solve simultaneous equations where one is linear and one quadratic or a circle

## 户. hegartymaths <br> Watch clip number \#246 <br> Or Corbett Maths \#298

## Practice Exercise 5.3

Complete these questions on file paper.
1 Solve these simultaneous equations.
a $y=2 x$ and $y=2 x^{2}$
b $y=x+3$ and $y=x^{2}+3 x$
c $y=3 x-1$ and $y=x^{2}-5$
d $y=6-x^{2}$ and $y=4 x+1$

2 Solve
a $y-3 x=4$ and $y=2 x^{2}-5$
b $x+y=2$ and $y=3 x^{2}-2$
c $y+2 x=5$ and $y=2 x^{2}+x$
d $x-y=3$ and $y=x^{2}-2 x-1$
e $2 x-y=-8$ and $y=x^{2}$
f $2 x+3 y=13$ and $y=x^{2}-1$

Mark your work.

## 4. Solve simultaneous equations graphically

## 穴 hegartymaths

Watch clip number \#218-219 \& \#259
Or Corbett Maths \#297

## Practice Exercise 5.4

Complete these questions on squared paper.

1. The diagrams show six lines labelled $L_{1}, L_{2}, L_{3}, L_{4}, L_{5}$ and $L_{6}$.




Use the diagrams to solve these simultaneous equations.
i $\begin{aligned} x & +y=3 \\ y & =x+1\end{aligned}$
ii $x+y=4$ $y=3 x-4$
iii $y=x-2$
$y=4 x-5$

Solve these simultaneous equations by drawing both graphs on one set of axes (from -5 to 5 ) and finding the point of intersection:
$2 \begin{array}{r}x+y=0 \\ y=x+2\end{array}$
$3 \begin{aligned} y & =x-2 \\ y & =2 x\end{aligned}$
$4 \begin{aligned} & x+y=1 \\ & y=-2 x-1\end{aligned}$
$5 y=x+1$
$y=2 x+4$
$6 y=2 x-5$
$x+y=4$

Solve these simultaneous equations by drawing both graphs on one set of axes and finding the points of intersection, remembering to pair up the values correctly:
7. a $y=3$ and $y=x^{2}+2 x$
b $y=5$ and $y=x^{2}-4 x$
c $y=-4$ and $y=x^{2}-5 x$
d $y=-1$ and $y=2 x^{2}+5 x+1$
8. a $y=x+6$ and $y=x^{2}$
b $y=x$ and $y=x^{2}-2$
c $y=x+1$ and $y=2 x^{2}$
d $y=4-x$ and $y=2 x^{2}+3$
e $y=x$ and $y=x^{2}+7 x+5$
f $x+2 y=0$ and $y=2 x^{2}-4 x-1$

Mark your work.

## GCSE to A Level Mathematics @ Ripley St Thomas



## Bridging Unit 6 - Inequalities

You need to be able to confidently:

- Solve linear inequalities
- Solve quadratic inequalities
- Plot a region using inequalities on a graph


## 1. Solve linear inequalities

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Watch clip number \#169-172

Or Corbett Maths \#178-179

## Practice Exercise 6.1

Complete these questions on file paper.
Solve each of the inequalities below:
1.
(a) $2 x+1 \leq 9$
(b) $3 x-5>16$
(c) $4 x+8<32$
(d) $5 x-2 \geq 68$
(e) $\frac{x}{2}+1 \leq 5$
(f) $\frac{x}{9}-6>4$
(g) $\frac{x+3}{2} \geq 5$
(h) $\frac{x-5}{4}>2$
2.
(a) $5(x-3) \geq 40$
(b) $6(x+2)<42$
(c) $2(5 x+1) \leq 36$
(d) $4(x-2)<18$
(e) $2(2 x-9) \geq 22$
(f) $3(2 x+7) \leq 9$
3.
(a) $4 x+3>2 x+11$
(b) $x+1 \geq 3 x-18$
(c) $13 x-12<3 x+13$
(d) $7 x-5 \geq 3 x+11$
4.
(a) $6<x+3<10$
(b) $4 \leq 2 x \leq 7$
(c) $1 \leq 3 x<9$
(d) $4<\frac{x}{5}<6$
(e) $9 \leq 2 x+3 \leq 25$
(f) $-3 \leq \frac{x}{4}-1<0$

Mark your work.

## 2. Solve quadratic inequalities

## 穴hegartymaths <br> Watch clip number \#277 <br> Or Corbett Maths \#378

## Practice Exercise 6.2

Complete these questions on file paper.
Solve the following inequalities:

1. (a) $(x-4)(x-1)<0$
(b) $(x-2)(x+1)<0$
(c) $(x+7)(x+3) \leq 0$
(d) $(x-5)(x+4) \leq 0$
(e) $x(x-9)>0$
(f) $(x+6)(x-5)>0$
(g) $(x+10)(x+1) \geq 0$
(h) $(x-7)(x+7) \geq 0$
(i) $(x+8)(x+2)<0$
(a) $x^{2}+5 x+6>0$
(b) $\mathrm{x}^{2}+7 \mathrm{x}+10<0$
(c) $x^{2}-4 x-5 \leq 0$
(d) $x^{2}+2 x-24>0$
(e) $x^{2}-6 x+8 \geq 0$
(f) $x^{2}+3 x-4<0$
(g) $x^{2}-x-56>0$
(h) $\mathrm{x}^{2}+9 \mathrm{x}+18<0$
(i) $\mathrm{x}^{2}-13 \mathrm{x}+22 \leq 0$
2. 

(a) $\mathrm{x}^{4}-1$
(b) $y^{4}-16$
(c) $\mathrm{a}^{4}-25$
(d) $x^{4}-y^{4}$
(e) $\mathrm{h}^{2}-\mathrm{p}^{4}$
(f) $16 x^{4}-49$
(g) $y^{6}-36$
(h) $x^{6}-64$
(i) $81 p^{4}-x^{6}$
(j) $144 \mathrm{x}^{8}-1$

Mark your work.

## 3. Factorise a quadratic where $\mathbf{a} \neq 1$

## 良hegartymaths

Watch clip number \#225
Or Corbett Maths \#119

## Practice Exercise 1.3

Complete these questions on file paper.
Factorise these expressions:
1.
(a) $2 x^{2}+7 x+5$
(b) $2 x^{2}+11 x+15$
(c) $2 x^{2}+9 x+10$
(d) $3 x^{2}+13 x+4$
(e) $3 x^{2}+4 x+1$
(f) $3 x^{2}+8 x+4$
2.
(a) $3 x^{2}+x-4$
(b) $7 x^{2}+20 x-3$
(c) $2 x^{2}-13 x+15$
(d) $3 x^{2}-17 x+10$
(e) $3 x^{2}-16 x-12$
(f) $3 x^{2}-x-4$
3.
(a) $6 x^{2}+13 x+6$
(b) $9 x^{2}+9 x+2$
(c) $6 x^{2}+13 x+2$
(d) $8 x^{2}+41 x+5$
(e) $9 x^{2}+6 x+1$
(f) $8 x^{2}+26 x+15$
4.
(a) $9 x^{2}-12 x-5$
(b) $4 x^{2}-4 x-3$
(c) $4 x^{2}-11 x+6$
(d) $6 x^{2}-7 x+2$
(e) $10 x^{2}-91 x+9$
(f) $4 x^{2}+25 x-56$

Mark your work.

## GCSE to A Level Mathematics @ Ripley St Thomas



## Bridging Unit 7 - Trigonometry

You need to be able to confidently:

- Find sides and angles in triangles using SOHCAHTOA in 2d and 3d
- Find angles, sides and areas in triangles using the Sine, Cosine and Area rules

1. Find sides and angles in triangles using SOHCAHTOA in 2d and 3d

## 官 hegartymaths

Watch clip number \#509 \& \#511

Or Corbett Maths \#330-332

## Practice Exercise 5.1

Complete these questions on file paper.

1. Find the lengths of the lettered sides in these triangles:
a

b

c


e

f

2. Find the length of $B C$ in these triangles:
a

b

3. Find the marked angle in these triangles:
a

d

b

c

e

f

4. The diagram shows a square-based pyramid. The lengths of sides of the square base, $A B C D$, are 10 cm and the base is on a horizontal plane.
The centre of the base is the point $M$ and the vertex of the pyramid is $O$, so that $O M$ is vertical.
The point $E$ is the midpoint of the side $A B$.
$O A=O B=O C=O D=15 \mathrm{~cm}$.
a Calculate the length of i $A C$ ii $A M$.
b Calculate the length of $O M$.
c Calculate the size of angle $O A M$.
d Hence find the size of angle $A O C$.
e Calculate the length of $O E$.
f Calculate the size of angle $O A B$.

5. $\quad A B C D$ is a horizontal rectangular lawn in a garden and $T C$ is a vertical pole. Ropes run from the top of the pole, $T$, to the corners, $A, B$ and $D$, of the lawn.
a Calculate the length of the rope $T A$.
b Calculate the size of the angle made with the lawn by
i the rope $T B$
ii the rope $T D$
iii the rope $T A$.


Mark your work.

## 2. Find angles, sides and areas in triangles using the Sine, Cosine and Area rules

## 户口 hegartymaths

Watch clip number \#516, \#521, \#523, \#527, \#529
Or Corbett Maths \#333-337

## Practice Exercise 5.2

Complete these questions on file paper.

1. Find the lengths of the sides marked with letters in these triangles.
a

b

c

2. Calculate the size of each of the acute angles marked with a letter.
a

b


3. Calculate the length of the sides marked with letters in these triangles.
a

b

c

4. Calculate the size of each of the angles marked with a letter in these triangles.
a

b

c

5. i

ii

6. The area of triangle $A B C$ is $15 \mathrm{~cm}^{2}$ Angle $A$ is acute. Work out the size of angle $A$.

7. The area of triangle $A B C$ is $60.7 \mathrm{~m}^{2}$ Work out the length of $B C$.

8. $A B C D$ is a kite with diagonal $D B$.
a Calculate the length of $D B$.
b Calculate the size of angle $B D C$.
c Calculate the value of $x$.
d Calculate the length of $A C$.


Mark your work.

## Unit 1 - Answers

## Practice Exercise 1.1

1. a) $(x+3)(x+4)$
b) $(x+4)(x+2)$
c) $(x+3)(x+2)$
d) $(x+7)(x+1)$
e) $(x+2)^{2}$
f) $(x+3)(x+5)$
g) $(x+3)^{2}$
h) $(x+7)(x+4)$
2. a) $(x+4)(x-3)$
b) $(x+6)(x-1)$
c) $(x+5)(x-2)$
d) $(x+4)(x-1)$
e) $(x+8)(x-6)$
f) $(x+8)(x-4)$
g) $(x+7)(x-5)$
h) $(x+11)(x-3)$
3. a) $(x-5)(x+2)$
b) $(x-5)(x+4)$
c) $(x-9)(x+3)$
d) $(x-3)(x+1)$
e) $(x-4)(x+3)$
f) $(x-6)(x+2)$
g) $(x-7)(x+3)$
h) $(x-11)(x+5)$
4. a) $(x-3)^{2}$
b) $(x-5)(x-4)$
c) $(x-7)(x-2)$
d) $(x-11)(x-2)$
e) $(x-8)(x-1)$
f) $(x-8)(x-4)$
g) $(x-7)(x+2)$
h) $(x-6)(x-8)$
5. a) $(x-8)(x-1)$
e) $(x+6)^{2}$
b) $(x+23)(x+1)$
C) $(x-7)(x+2)$
d) $(x-3)(x-4)$
f) $(x-9)(x+7)$
g) $(x+13)(x+2)$
h) $(x+12)(x+5)$

## Practice Exercise 1.2

1. a) $(x+5)(x-5)$
b) $(y+7)(y-7)$
C) $(w+10)(w-10)$
d) $(x+2)(x-2)$
e) $(c+8)(c-8)$
f) $(x+1)(x-1)$
g) $(x+30)(x-30)$
h) $(y+3)(y-3)$
i) $(16+x)(16-x)$
j) $(1+y)(1-y)$
k) $(9+x)(9-x)$
I) $(12+h)(12-h)$
m) $(x+y)(x-y)$
n) $(a+c)(a-c)$
o) $(3 x+5)(3 x-5)$
p) $(2 x+1)(2 x-1)$

## 2.

a) $\left(x^{2}+1\right)\left(x^{2}-1\right)$
b) $\left(x^{2}+1\right)\left(x^{2}-1\right)$
c) $\left(a^{2}+5\right)\left(a^{2}-5\right)$
d) $\left(x^{2}+y^{2}\right)\left(x^{2}-y^{2}\right)$
e) $\left(h+p^{2}\right)\left(h-p^{2}\right)$
f) $\left(4 x^{2}+7\right)\left(4 x^{2}-7\right)$
g) $\left(y^{3}+6\right)\left(y^{3}-6\right)$
h) $\left(x^{3}+8\right)\left(x^{3}-8\right)$
i) $\left(9 p^{2}+x^{3}\right)\left(9 p^{2}-x^{3}\right)$
j) $\left(12 x^{4}+1\right)\left(12 x^{4}-1\right)$

## Practice Exercise 1.3

1. 

a) $\quad(2 x+5)(x+1)$
b) $\quad(2 x+5)(x+3)$
c) $\quad(2 x+5)(x+2)$
d) $(3 x+1)(x+4)$
e) $\quad(3 x+1)(x+1)$
f) $\quad(3 x+2)(x+2)$
2.
a) $(3 x+4)(x-1)$
b) $\quad(7 x-1)(x+3)$
c) $\quad(2 x-3)(x-5)$
d) $(3 x-2)(x-5)$
e) $\quad(3 x+2)(x-6)$
f) $\quad(3 x-4)(x+1)$
3.
a) $\quad(3 x+2)(2 x+3)$
b) $\quad(3 x+2)(3 x+1)$
c) $\quad(6 x+1)(x+2)$
d) $(8 x+1)(x+5)$
e) $\quad(3 x+1)^{2}$
f) $(4 x+3)(2 x+5)$
4.
a) $\quad(3 x+1)(3 x-5)$
b) $\quad(2 x+1)(2 x-3)$
c) $(4 x-3)(x-2)$
d) $(2 x-1)(3 x-2)$ e) $(10 x-1)(x-9)$ f) $(4 x-7)(x+8)$

## Practice Exercise 1.4

1. 

a) $\quad x=-4$ or $x=-2$
b) $\quad x=-4$ or $x=-3$
c) $\quad x=-5$ or $x=-2$
d) $\quad x=-4$ or $x=1$
e) $\quad x=-2$ or $x=$
f) $\quad x=3$ or $x=4$
g) $\quad x=5$
h) $\quad x=-5$ or $x=9$ i
i) $\quad x=-7$ or $x=8$
2.
a) $\quad x= \pm 3$
b) $\quad x= \pm 10$
c) $\quad x= \pm 1$
d) $x= \pm 12$
e) $\quad x= \pm 8$
f) $\quad x= \pm 0.5$
3.
a) $\quad x=-1$
b) $\quad x=-7$ or $x=-1$
c) $\quad x=3$ or $x=4$
d) $\quad x=-12$ or $x=-1$
e) $\quad x=-2$ or $x=5$
f) $x=7$

## Practice Exercise 1.5

1. 

a) $\quad(x+4)^{2}-15$
b) $\quad(x+5)^{2}-22$
c) $\quad(x+1)^{2}-2$
d) $\quad(x-3)^{2}-19$
e) $\quad(x-2)^{2}-17$
f) $\quad(x-6)^{2}-33$
g) $\quad(x+7)^{2}-46$
h) $\quad(x-1)^{2}-16$
i) $\quad(x+2)^{2}-15$
j) $\quad\left(x+\frac{1}{2}\right)^{2}-\frac{35}{4}$
k) $\quad\left(x+\frac{3}{2}\right)^{2}-\frac{5}{4}$
I) $\quad\left(x-\frac{7}{2}\right)^{2}-\frac{57}{4}$
2.
a) $\quad 2(x+4)^{2}-30$
b) $\quad 2(x+3)^{2}-21$
c) $\quad 3(x-2)^{2}-10$
d) $\quad 4\left(x+\frac{3}{2}\right)^{2}-14$
e) $2\left(x-\frac{3}{4}\right)^{2}-\frac{49}{8}$
f) $\quad 5(x-2)^{2}+10$

## Practice Exercise 1.6

1. 

a) $\quad x=-4$ or $x=-2$
b) $\quad x=-6$ or $x=-4$
c) $\quad x=-10$ or $x=-4$
d) $\quad x=-5$ or $x=9$
e) $\quad x=5$ or $x=7$
f) $\quad x=3$ or $x=-1$
2.
a) $\quad x=-4$ or $x=-1$
b) $\quad x=-3$ or $x=6$
c) $\quad x=-4$ or $x=3$
d) $\quad x=3$ or $x=4$
e) $\quad x=3$ or $x=8$
f) $\quad x=-3$ or $x=10$
3.
a) $(x+2)^{2}-7=0$ $(x+2)^{2}=7$
$x+2= \pm \sqrt{ } 7$
b) $(x+3)^{2}-19=0$
$(x+3)^{2}=19$
$x+3= \pm \sqrt{ } 19$
$x=-3 \pm \sqrt{ } 19$
c) $(x-1)^{2}-6=0$
$(x-1)^{2}=6$
$x-1= \pm \sqrt{6}$
$x=1 \pm \sqrt{ } 6$
d) $(x-5)^{2}-24=0$ $(x-5)^{2}=24$
$x-5= \pm \sqrt{ } 24$
$x=5 \pm \sqrt{ } 24$
e) $(x+4)^{2}-13=0$
$(x+4)^{2}=13$
$x+4= \pm \sqrt{ } 13$
$x=-4 \pm \sqrt{ } 13$
f) $(x-4)^{2}-38=0$
$(x-4)^{2}=38$
$x-4= \pm \sqrt{38}$
$x=4 \pm \sqrt{ } 38$
4. a) $5\left(x^{2}+6 x\right)-10=0$

$$
5(x+3)^{2}-55=0
$$

$$
5(x+3)^{2}=55
$$

$$
(x+3)^{2}=1
$$

$$
x+3= \pm \sqrt{ } 1
$$

$$
x=-4 \text { or } x=-2
$$

d) $2\left(x^{2}-\frac{3}{2} x\right)-7=0$

$$
2\left(x-\frac{3}{4}\right)^{2}-\frac{65}{8}=0
$$

$$
2\left(x-\frac{3}{4}\right)^{2}=\frac{65}{8}
$$

$$
\left(x-\frac{3}{4}\right)^{2}=\frac{65}{16}
$$

$$
x-\frac{3}{4}= \pm \sqrt{ } \frac{65}{16}
$$

$$
x=\frac{3 \pm \sqrt{ } 65}{4}
$$

b) $2\left(x^{2}+\frac{7}{2} x\right)+3=0$
$2\left(x+\frac{7}{4}\right)^{2}-\frac{25}{8}=0$
$2\left(x+\frac{7}{4}\right)^{2}=\frac{25}{8}$
$\left(x+\frac{7}{4}\right)^{2}=\frac{25}{16}$
$x+\frac{7}{4}= \pm \sqrt{\frac{25}{16}}$
$x=-\frac{1}{4}$ or $x=-\frac{11}{4}$
e) $5\left(x^{2}+\frac{2}{5} x\right)-8=0$
$5\left(x+\frac{1}{5}\right)^{2}-\frac{41}{5}=0$
$5\left(x+\frac{1}{5}\right)^{2}=\frac{41}{5}$
$\left(x+\frac{1}{5}\right)^{2}=\frac{41}{25}$
$x+\frac{1}{5}= \pm \sqrt{41} \frac{1}{25}$
$x=\frac{-1 \pm \sqrt{ } 41}{25}$
$3(x+2)^{2}-14=0$
$3(x+2)^{2}=14$
$(x+2)^{2}=\frac{14}{3}$
$x+2= \pm \sqrt{\frac{14}{3}}$
$x=-2 \pm \sqrt{\frac{14}{3}}$
c) $3\left(x^{2}+4 x\right)-2=0$
f) $10\left(x^{2}-\frac{1}{5} x\right)-1=0$
$10\left(x-\frac{1}{10}\right)^{2}-\frac{11}{10}=0$
$10\left(x-\frac{1}{10}\right)^{2}=\frac{11}{10}$
$\left(x-\frac{1}{10}\right)^{2}=\frac{11}{100}$
$x-\frac{1}{10}= \pm \sqrt{\frac{11}{100}}$
$x=\frac{1 \pm \sqrt{ } 11}{100}$

## Unit 2 Answers

## Exercise 2.1

1. $y=x^{2}-4$
2. $y=x^{2}+2 x$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 5 | 0 | -3 | -4 | -3 | 0 | 5 |


| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 3 | 0 | -1 | 0 | 3 | 8 | 15 |


3. $y=5 x-x^{2}$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | -24 | -14 | -6 | 0 | 4 | 6 | 6 |

4. $y=x^{2}+4 x+7$

| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 4 | 3 | 4 | 7 | 12 | 19 | 28 |




## Exercise 2.2

1. 


3.

4.


## Answers to Exercise 2.3

1. $y=(x-4)^{2}-5$
2. $y=(x-3)(x+5)$
3. $y=(x+2)^{2}+3$
4. $y=(x-1)(x-3)$

## Unit 3 - Answers

## Exercise 3.1

1. a) Gradient $=7, y$-intercept $=-8$
b) Gradient $=2, \quad y$-intercept $=9$
c) Gradient $=0.5, y$-intercept $=0$
2. a) $y=5 x-2$
b) $y=10 x+7$
c) $y=-3 x+1$
3. 



1b)



2a)


2b)


2c)

4. a) $y=3 x-2$
b) $y=-x+3$
c) $y=-2 x+4$
d) $y=0.5 x+2$

## Exercise 3.2

1. $y=-x+13$

Gradient $=-1, \quad y$-intercept $=13$
2. $y=4 x+6$
3. $y=2 x+7$
4. $y=-2 x+\frac{5}{2}$
5. $y=-\frac{1}{4} x+5$

Gradient $=4, \quad y$-intercept $=6$
Gradient $=2, \quad y$-intercept $=7$
Gradient $=-2, \quad y$-intercept $=\frac{5}{2}$
6. $y=3 x-\frac{3}{2}$

Gradient $=-\frac{1}{4}, \quad y$-intercept $=5$
7. $y=18 x-9$

Gradient $=3, \quad y$-intercept $=-\frac{3}{2}$
8. $y=\frac{6}{7} x+1$
9. $y=\frac{6}{5} x-\frac{12}{5}$

Gradient $=18, \quad y$-intercept $=-9$
10. $y=\frac{6}{5} x-\frac{4}{5}$

Gradient $=\frac{6}{7}, \quad y$-intercept $=1$
Gradient $=\frac{6}{5}, \quad y$-intercept $=-\frac{12}{5}$
Gradient $=\frac{6}{5}, \quad y$-intercept $=-\frac{4}{5}$

## Exercise 3.3

1. $y=3 x-1$
2. $y=7 x+21$
3. $y=-2 x+8$
4. $y=-10 x-25$
5. $y=3 x+4$
6. $y=2 x+6$
7. $y=2 x-2$
8. $y=\frac{1}{2} x-\frac{17}{2}$
9. $y=4 x-11$
10. $y=-x-4$
11. $y=x+7$
12. $y=\frac{1}{2} x+7$

## Exercise 3.4

1. $y=-\frac{1}{2} x+4$
2. $y=\frac{1}{3} x+\frac{5}{3}$
3. $y=-2 x+18$
4. $y=-8 x-4$
5. $y=\frac{3}{2} x-\frac{19}{2}$

## Unit 4 - Answers

## Practice Exercise 4.1a

| 1 a $2^{9}$ | b $2^{7}$ | c $2^{8}$ | d $2^{7}$ | e $2^{10}$ |
| :---: | :---: | :---: | :---: | :---: |
| 2 a $3^{2}$ | b $3^{3}$ | c $3^{3}$ | d $3^{4}$ | e $3^{6}$ |
| 3 a $4^{2}$ | b $5^{5}$ | c $3^{6}$ | d $6^{7}$ | e $10^{2}$ |
| 4 a 5 | b 3 | c 5 | d 4 | e 9 |
| 5 a 9 | b 16 | c 8 | d $10^{6}$ | e 6 |
| 6 a $3^{4}$ | b $3^{6}$ | c $3^{4}$ | d $3^{2}$ | e $3^{5}$ |
| 7 a $2^{2}$ | b $3^{3}$ | c $5^{2}$ | d $10^{4}$ | e $4^{4}$ |
| 8 a 5 | b 1 | c 16 | d 2 | e 9 |
| 9 a 3 | b 5 | c 2 | d 4 | e 3 |

## Practice Exercise 4.1b



## Practice Exercise 4.2a

| 1 a $\frac{1}{2}$ | b $\frac{1}{9}$ |  | C $\frac{1}{5}$ |  | $\frac{1}{1000}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| e 1 | f $\frac{2}{5}$ |  | g 3 |  | h $\frac{9}{4}$ |
| 2 a $\frac{1}{3}$ | b $\frac{1}{4}$ | C | 25 d | d $\frac{1}{36}$ | e $\frac{1}{8}$ |
| 3 a $\frac{1}{4}$ | b 27 | c | 4 d | d $\frac{1}{10}$ | e $\frac{1}{25}$ |
| 4 a $\frac{1}{2}$ | b $\frac{1}{3}$ | c | $\frac{1}{5}$ d | d 16 | e 32 |
| 5 a $\frac{1}{2}$ | b $\frac{1}{9}$ | C | 5 d | d 64 | e 1 |
| 6 a -3 | b -3 |  | c -2 | d | -6 |
| 7 a 700 | b 200000 |  | c 4900 | d 0.8 | e 0.0069 |
| 8 a 3 | b 4 |  | c -1 |  | $-2$ |
| 9 a 0.8 | b 6.25 | C | 6.25 d | d 0.064 | e 0.0064 |
| 10 a 2.22 | b 0.198 |  | c 1.13 |  | 30800 |

## Practice Exercise 4.2b

| $\mathbf{1}$ | a 3 | b 5 | c 10 | d 2 | e $\frac{1}{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2}$ | a 3 | b 10 | c -4 | d 5 | e $\frac{1}{5}$ |
| $\mathbf{3}$ | a $\frac{1}{16}$ | b $\frac{1}{9}$ | c $\frac{4}{9}$ | d $\frac{4}{25}$ | e $\frac{27}{64}$ |
| 4 a 9 | b 100 | c 16 | d 8 | e 125 |  |
| $\mathbf{5}$ a $\frac{1}{5}$ | b $\frac{1}{3}$ | c $\frac{1}{3}$ | d $\frac{1}{4}$ | e $\frac{1}{512}$ |  |
| $\mathbf{6}$ a $-\frac{1}{2}$ |  | b $\frac{5}{2}$ | c $\frac{11}{3}$ |  |  |

## Practice Exercise 4.3

1 a 2
b 3
c 5
d 4
e 6
2 a $3+2 \sqrt{3}$
b $5+3 \sqrt{3}$
c $3+\sqrt{5}$
d -12
e $7-4 \sqrt{3}$
3 a $\frac{\sqrt{2}}{2}$
b $\frac{\sqrt{5}}{5}$
c $\frac{2 \sqrt{7}}{7}$
d $\frac{3 \sqrt{2}}{2}$
e $\frac{5 \sqrt{11}}{11}$
4 a $\frac{\sqrt{6}}{3}$
b $\frac{\sqrt{3}}{2}$
c $\frac{\sqrt{10}}{2}$
d $\sqrt{2}$
e $2 \sqrt{5}$
5 a $1+\sqrt{2}$
b $\sqrt{2}-1$
c $1+2 \sqrt{5}$
d $\sqrt{5}-1$
e $2 \sqrt{7}+1$
64 cm
$73+2 \sqrt{2} \mathrm{~cm}^{2}$
8 a i 14 cm
ii $7+\sqrt{5} \mathrm{~cm}^{2}$

## Unit 5 - Answers

## Practice Exercise 5.1

1. (a) $x=2$
$y=6$
(b) $x=1$
$y=3$
(c) $x=3$
$y=2$
(d) $x=15$
$y=6$
(e) $x=5$
$y=6$
(f) $x=3$ $y=0.5$
2. (a) $x=5$
$y=4$
(b) $x=5$ $y=2$
(c) $x=4$
$y=9$
(d) $\begin{aligned} x & =11 \\ y & =10\end{aligned}$
(e) $x=7.5$
$y=3.5$
(f) $x=7$ $y=1$
3. 

(a) $x=5$
$y=2$
(b) $x=-4$
$y=3$
(c) $x=2$ $y=4$
(d) $x=8$
(e) $x=-1$
(f) $x=-4$ $y=2$

## Practice Exercise 5.2

1. (a) $x=-5$ and $y=-2, \quad x=1$ and $y=4$
(b) $x=-3$ and $y=-8, x=3$ and $y=-2$
(c) $x=1$ and $y=1, x=3$ and $y=5$
(d) $x=-4$ and $y=-3, x=1$ and $y=12$
(e) $x=-4$ and $y=29, x=-2$ and $y=7$
(f) $x=-0.5$ and $y=-0.75, x=2$ and $y=8$
2. (a) $x=-5$ and $y=9, x=1$ and $y=3$
(b) $x=2$ and $y=5, x=5$ and $y=2$
(c) $x=2$ and $y=3, x=3$ and $y=2$
(d) $x=-2$ and $y=0, \quad x=3$ and $y=10$
(e) $x=-5$ and $y=-2, x=-2$ and $y=-5$
(f) $x=-6$ and $y=1, x=2$ and $y=-3$
3. (a) $x=3$ and $y=1, x=6.333 \ldots$ and $y=-5.666 .$.
(b) $x=-4.284$ and $y=-1.284, x=1.284$ and $y=4.284$
(c) $x=-0.2915$ and $y=-0.2915, x=10.2915$ and $y=10.2915$
(d) $x=1.14$ and $y=-2.72, x=2.19$ and $y=-0.613$
(e) $x=-4.46$ and $y=8.42, x=1.46$ and $y=-3.42$
(f) $x=-4.46$ and $y=-6.46, x=2.46$ and $y=0.46$

## Practice Exercise 5.3

1 a $x=0, y=0$ or $x=1, y=2$
b $x=1, y=4$ or $x=-3, y=0$
c $x=4, y=11$ or $x=-1, y=-4$
d $x=1, y=5$ or $x=-5, y=-9$
2 a $x=3, y=13$ or $x=-1.5, y=-0.5$
b $x=1, y=1$ or $x=-\frac{4}{3}, y=\frac{10}{3}$
c $x=1, y=3$ or $x=-\frac{5}{2}, y=10$
d $x=2, y=-1$ or $x=1, y=-2$
e $x=4, y=16$ or $x=-2, y=4$
f $x=2, y=3$ or $x=-\frac{8}{3}, y=\frac{55}{9}$

## Practice Exercise 5.4

1. i $x=1, y=2 \quad$ ii $x=2, y=2 \quad$ iii $x=1, y=-1$
$2 x=-1, y=1$
$3 x=-2, y=-4$
$4 x=-2, y=3$
$5 x=-3, y=-2$ $6 x=3, y=1$
2. 

a) $x=1, y=3$ or $x=-3, y=3$
b) $\quad x=5, y=5$ or $x=-1, y=5$
c) $x=1, y=-4$ or $x=4, y=-4$
d) $x=-2, y=-1$ or $x=-0.5, y=-1$

## 8.

a) $x=3, y=9$ or $x=-2, y=4$
b) $\quad x=2, y=2$ or $x=-1, y=-1$
c) $x=1, y=2$ or $x=-0.5, y=0.5$
d) $x=-1, y=5$ or $x=0.5, y=3.5$
e) $x=-1, y=-1$ or $x=-5, y=-5$
f) $x=-2, y=-1$ or $x=-0.25, y=0.125$

## Unit 6 - Answers

## Practice Exercise 5.1

1. a 5.47 cm
b 17.1 cm
c 11.6 cm
d 7.79 cm
e 25.5 cm
f 9.18 cm
2. a 24.2 cm
b 29.6 cm
3. a $37.7^{\circ}$
b $46.2^{\circ}$
c $19.7^{\circ}$
d $45.6^{\circ}$
e $47.1^{\circ}$
f $43.6^{\circ}$
4. a 13 cm
b i 19.8 cm
ii 19.2 cm
c i $67.4^{\circ}$
ii $38.7^{\circ}$
5. a 15.6 m
b i $26.6^{\circ}$
ii $36.9^{\circ}$
iii $22.6^{\circ}$

## Practice Exercise 5.2

1. a 8.06 cm
b 7.19 cm
c 6.35 cm
2. a $45.0^{\circ}$
b $63.6^{\circ}$
c $23.6^{\circ}$
3. a 8.79 cm
b 12.6 cm
c 5.01 cm
4. a $54.7^{\circ}$
b $81.2^{\circ}$
c $46.0^{\circ}$
5. $\mathbf{i} 21.9 \mathrm{~cm}^{2}$
ii $29.2 \mathrm{~cm}^{2}$
6. $33.3^{\circ}$
7. $16.8 \mathrm{~m}^{2}$
8. a 6.76 cm
b $75^{\circ}$
c 13.1 cm
d 19.9 cm


## This section of the Bridging Unit is compulsory and must be handed in during your first Mathematics lesson.

You are expected to submit this homework in during the first Mathematics lesson after the summer holidays. In the new academic year you will sit a test as part of the transition period. The test will focus on many of the skills included in this booklet. The knowledge and skills assessed in this booklet, and on the induction test, are required for success in A-Level Mathematics. Therefore, it is essential that you are confident in all the skills included in this booklet.

Success in A-Level Mathematics relies on an excellent attitude to learning and commitment to your studies. If you are struggling with any of the content in this book, you must use the video links included to brush up on these key skills. The videos stated are accessible on www.hegartymaths.com (if you have access to this through your current school) OR www.corbettmaths.com (for everyone).

You are expected to write neatly, show the method clearly. Diagrams should be drawn using a pencil and ruler.

## Content

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## LAWS OF INDICES

Hegarty Maths No: 102-110
Corbett Maths: 173, 174, 176

1. (a) Simplify $m^{5} \div m^{3}$
(b) Simplify $5 x^{4} y^{3} \times x^{2} y$
2. Write these numbers in order of size.

Start with the smallest number.
$5^{-1}$
0.5
$-5$
$5^{0}$
3. Write down the value of $125^{\frac{2}{3}}$
4. (a) Find the value of $5^{0}$
(b) Find the value of $27^{1 / 3}$
(c) Find the value of $2^{-3}$
5. (a) Write down the value of $64^{\frac{1}{2}}$
(b) Find the value of $\left(\frac{8}{125}\right)^{-\frac{2}{3}}$

## SURDS

Hegarty Maths No: 115-119, 500
Corbett Maths: 305-308

1. Write $\frac{\sqrt{18}+10}{\sqrt{2}}$ in the form $a+b \sqrt{ } 2$ where $a$ and $b$ are integers.
2. (a) Rationalise the denominator of $\frac{1}{\sqrt{3}}$
(b) Expand $(2+\sqrt{3})(1+\sqrt{3})$ Give your answer in the form $a+b \sqrt{3}$ where $a$ and $b$ are integers.
3. Work out

$$
\frac{(5+\sqrt{3})(5-\sqrt{3})}{\sqrt{22}}
$$

Give your answer in its simplest form.
3. (a) Rationalise the denominator of $\frac{1}{\sqrt{7}}$
(b) (i) Expand and simplify $(\sqrt{3}+\sqrt{15})^{2}$

Give your answer in the form $a+b \sqrt{3}$ where $a$ and $b$ are integers.
(ii) All measurements on the triangle are in centimetres.
$A B C$ is a right-angled triangle.
$k$ is a positive integer.


Diagram NOT
accurately drawn

Find the value of $k$.

$$
k=
$$

## CHANGING THE SUBJECT FOR A FORMULA

Hegarty Maths No: 280-286
Corbett Maths: 7, 8

1. Make $u$ the subject of the formula

$$
D=u t+k \mathrm{t}^{2}
$$

$$
u=
$$

2. Rearrange $(q-c)=d$ to make $q$ the subject.

$$
q=
$$

3. Make $x$ the subject of

$$
5(x-3)=(4-3 x)
$$

$$
x=
$$

4. Rearrange the formula to make $a$ the subject.

$$
P=\frac{n^{2}+a}{n+a}
$$

## SIMULTANEOUS EQUATIONS (LINEAR AND NON-LINEAR)

Hegarty Maths No: 192-194, 218-219, 246, 259
Corbett Maths: 295-298

1. Use the axes provided to solve the simultaneous equations.

$$
y=2 x-1 \text { and } y=7-x
$$


2. Solve the simultaneous equations
(a) $3 x+4 y=5$
(b) $2 x+3 y=\frac{2}{3}$
$2 x-3 y=9$
$3 x-4 y=18$
$x=$ $\qquad$ $x=$
$y=$ $\qquad$

$$
y=
$$

$\qquad$
3. Solve the equations

$$
\begin{gathered}
x^{2}+y^{2}=36 \\
x=2 y+6
\end{gathered}
$$

$$
\begin{aligned}
& x= \\
& y=
\end{aligned}
$$

4. Solve the equations

$$
\begin{gathered}
x+y=4 \\
y=x^{2}+3 x-1
\end{gathered}
$$

$$
\begin{aligned}
& x= \\
& y=
\end{aligned}
$$

## EXPANDING AND FACTORISING QUADRATIC EXPRESSIONS/EQUATIONS

Hegarty Maths No: 162-164, 168-169, 223-228, 230-233
Corbett Maths: 118, 119, 119a

1. Expand and simplify $(m+7)(m+3)$
2. (a) Factorise $6+9 x$
(b) Factorise $y^{2}-16$
(c) Factorise $2 p^{2}-p-10$
3. (a) Factorise $x^{2}+5 x+4$
(b) Expand and simplify $(3 x-1)(2 x+5)$
4. (a) Factorise $x^{2}+7 x$
(b) Factorise $y^{2}-10 y+16$
(c) (i) Factorise $2 t^{2}+5 t+2$
5. Solve, by factorising, the equation $8 x^{2}+2 x-15=0$

## USING THE QUADRATIC FORMULA

Hegarty Maths No: 241-242
Corbett Maths: 267

1. Solve $3 x^{2}+7 x-13=0$

Give your solutions correct to 2 decimal places.

$$
x=
$$

or $x=$
2. Solve the equation

$$
2 x^{2}+6 x-95=0
$$

Give your solutions correct to 3 significant figures.

$$
x=
$$

or $x=$
3. Solve this quadratic equation. $x^{2}=5 x+8$

Give your answers correct to 3 significant figures.
$\qquad$

## COMPLETING THE SQUARE

Hegarty Maths No: 235-239
Corbett Maths: 267a, 265

1. The expression $x^{2}-8 x+21$ can be written in the form $(x+a)^{2}+b$ for all values of $x$.
(a) Find the value of $a$ and the value of $b$.
$\qquad$
$a=$
$b=$

The equation of a curve is $y=(x)$ where $(x)=x 2-8 x+21$
The diagram shows part of a sketch of the graph of $y=(x)$.


The minimum point of the curve is $M$.
(b) Write down the coordinates of $M$.
2. Sketch the graph of $(x)=x^{2}-5 x+10$, showing the coordinates of the turning point and the coordinates of any intercepts with the coordinate axes.
3. (a) Write $2 x^{2}+16 x+35$ in the form $a(x+b)^{2}+c$ where $a, b$, and $c$ are integers.
(b) Hence, or otherwise, write down the coordinates of the turning point of the graph of $y=2 x^{2}+16 x+35$

## INEQUALTIES

Hegarty Maths No: 270-277
Corbett Maths: 178, 179, 182

1. Find the range of values of $x$ that is satisfied by the following inequalities below.

You must show your working out.
(1 a) ve $8 x-3 \geq 9$
(2 b) ve $5(3 x-2) \leq 125$
(3 C) re $\frac{2 x-3}{5}>9$
$(4 \mathrm{~d})$ ve $3 / 8(5 x+1) \leq 66$
(5 e) ve $-7 \leq 5 x+3 \leq 23$
$(6 \mathrm{f})$ ve $1 \leq 6-5 x \leq 41$
2. For what values of $x$ is the perimeter of the square greater than the perimeter of the rectangle?

3. On the axes provided, draw straight lines, and use shading, to show the region R that satisfies the inequalities detailed.

$$
\begin{gathered}
y \geq x+1 \\
y \geq 5 \\
x \geq 1
\end{gathered}
$$


4. On the axes provided, draw straight lines, and use shading, to show the region R that satisfies the inequalities detailed.

$$
\begin{gathered}
y \geq x \\
x+y \leq 7 \\
x \geq 1
\end{gathered}
$$



