

Ripley St Thomas A-Level Maths

Bridging Provision

Introduction

In order to prepare for taking A-level maths next year, you need to ensure you are fluent in all aspect of GCSE, particularly algebra and those included in this booklet, and can approach problems with a confident, logical mindset.

You are expected to use this booklet to fill gaps in your knowledge, build confidence and ensure you start Alevel mathematics fully prepared. The knowledge and skills you find here, are essential for success in A-Level Mathematics.

The last 15 pages of this booklet are your first transition piece. This is **compulsory** and **must** be handed in during your first A-level mathematics lesson.

Success in A-Level Mathematics relies on an excellent attitude to learning and commitment to your studies. If you are struggling with any of the content in this booklet, you must use the video links included to brush up on these key skills. The videos stated are accessible on www.hegartymaths.com (if you have access to this through your current school) OR www.hegartymaths.com (if you have access to this through your current school) OR www.corbettmaths.com (for everyone).

PLEASE NOTE HEGARTY MATHS CEASES TO EXIST ON 31ST AUGUST. DO NOT LEAVE THIS DOCUMENT UNTIL THE DAY BEFORE YOU START SCHOOL.

Additional resources to help you prepare.

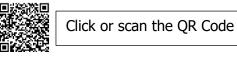
As mentioned above it is important that you start Year 12 with an excellent attitude and be prepared to go above what is necessarily set as independent learning tasks. There are plenty of resources available online, please below for a few extra ideas to help you prepare for A-Level Maths.

1. <u>Bridging the Gap</u> – An A-Level maths tutor who produces videos and online resources. This page gives you the basics and videos with a A-Level spin. We **do not** recommend paying £95 per hour for the 1-1 tuition.



Click or scan the QR Code

 <u>AMSP Transition to A-Level Essential Skills</u> – AMSP produce amazing resources and these were designed for students to complete independently and will develop fluency in the fundamental techniques and the key mathematical concepts that underpin A level Mathematics.



3. <u>Sparx Maths Transition Booklet</u> – If your school uses SPARX then you can use the codes in the transition booklet. Otherwise this is just additional maths practice linked to the beginnings of A-Level.



Click or scan the QR Code

4. <u>OCRs Bridging the gap</u> – Produced by OCR (an exam board) this is a bit more old school textbook style with examples and exercises. These have some tricky questions which will test your abilities well.



Click or scan the QR Code

5. <u>TL Maths</u> – This person produces very good videos for A-Level maths and he has made a series of bridging videos to help with the transition.



Click or scan the QR Code

Bridging Unit Content

Complete the 'RAG' table and use this as a starting point to direct your independent study. You can then revisit this and update your self-assessment as you grow in confidence.

	••	••
Quadratics		
Factorise a quadratic expression where $a = 1$		
Factorise a 'DOTS' type quadratic expression		
Factorise a quadratic expression where a $\neq 1$		
Solve a quadratic equation by factorising		
Write a quadratic expression in completed square form		
Solve a quadratic equation by completing the square		
Quadratic Graphs		
Complete a table of values and plot a quadratic graph		
Sketch a quadratic graph given its equation by:		
• Finding the <i>x</i> -intercept(s) (if any)		
• Finding the <i>y</i> -intercept		
Finding the coordinates of the vertex by writing in completed square form		
Write down the equation of a quadratic given the graph		
Linear Graphs		
Write the equation for/draw a straight line using the gradient and intercept		
Find the gradient and y-intercept of a line by rearranging its equation		
Find the equation of a line using gradient and coordinates		
Find the equation of a perpendicular line		
Surds and Indices		
Apply the Index Laws with numbers or algebra		
Work with negative and fractional indices		
Manipulate expressions containing surds (including simplifying surds, expanding brackets containing surds and rationalising a denominator)		
Simultaneous Equations		
Solve linear simultaneous equations by elimination		
Solve linear simultaneous equations by substitution		
Solve simultaneous equations where one is linear and one quadratic or a circle		
Solve simultaneous equations graphically		
Inequalities		
Solve linear inequalities		
Solve quadratic inequalities		
Plot a region using inequalities on a graph		
Trigonometry		
Find sides and angles in triangles using SOHCAHTOA in 2d and 3d		
Find angles, sides and areas in triangles using the Sine, Cosine and Area rules		



You need to be able to confidently:

- Factorise a quadratic expression where a = 1
- Factorise a 'DOTS' type quadratic expression
- Factorise a quadratic expression where a $\neq 1$
- Solve a quadratic equation by factorising
- Write a quadratic expression in completed square form
- Solve a quadratic equation by completing the square

1. Factorise a quadratic expression where a = 1



Watch clip number #223

Or Corbett Maths #118

Practice Exercise 1.1

Complete these questions on file paper. Factorise these expressions:

(a) $x^2 + 7x + 12$	(b) $x^2 + 6x + 8$	(c) $x^2 + 5x + 6$	(d) $x^2 + 8x + 7$
(e) $x^2 + 4x + 4$	(f) $x^2 + 8x + 15$	(g) $x^2 + 6x + 9$	(h) $x^2 + 11x + 28$
(a) $x^2 + x - 12$	(b) $x^2 + 5x - 6$	(c) $x^2 + 3x - 10$	(d) $x^2 + 3x - 4$
(e) $x^2 + 2x - 48$	(f) $x^2 + 4x - 32$	(g) $x^2 + 2x - 35$	(h) $x^2 + 8x - 33$
(a) $x^2 - 3x - 10$	(b) $x^2 - x - 20$	(c) $x^2 - 6x - 27$	(d) $x^2 - 2x - 3$
(e) $x^2 - x - 12$	(f) $x^2 - 4x - 12$	(g) $x^2 - 4x - 21$	(h) $x^2 - 6x - 55$
	(e) $x^{2} + 4x + 4$ (a) $x^{2} + x - 12$ (e) $x^{2} + 2x - 48$ (a) $x^{2} - 3x - 10$	(e) $x^{2} + 4x + 4$ (f) $x^{2} + 8x + 15$ (a) $x^{2} + x - 12$ (b) $x^{2} + 5x - 6$ (e) $x^{2} + 2x - 48$ (f) $x^{2} + 4x - 32$ (a) $x^{2} - 3x - 10$ (b) $x^{2} - x - 20$	(e) $x^{2} + 4x + 4$ (f) $x^{2} + 8x + 15$ (g) $x^{2} + 6x + 9$ (a) $x^{2} + x - 12$ (b) $x^{2} + 5x - 6$ (c) $x^{2} + 3x - 10$ (e) $x^{2} + 2x - 48$ (f) $x^{2} + 4x - 32$ (g) $x^{2} + 2x - 35$ (a) $x^{2} - 3x - 10$ (b) $x^{2} - x - 20$ (c) $x^{2} - 6x - 27$

4. (a) $x^{2} - 6x + 9$ (b) $x^{2} - 9x + 20$ (c) $x^{2} - 9x + 14$ (d) $x^{2} - 13x + 22$ (e) $x^{2} - 9x + 8$ (f) $x^{2} - 12x + 32$ (g) $x^{2} - 15x + 36$ (h) $x^{2} - 14x + 48$ 5. (a) $x^{2} - 9x + 8$ (b) $x^{2} + 24x + 23$ (c) $x^{2} - 5x - 14$ (d) $x^{2} - 7x + 12$ (e) $x^{2} + 12x + 36$ (f) $x^{2} - 2x - 63$ (g) $x^{2} + 14x + 24$ (h) $x^{2} + 17x + 60$

Mark your work.

2. Factorise a 'DOTS' quadratic expression

A hegartymaths

Watch clip number #224

Or Corbett Maths #120

Practice Exercise 1.2

Complete these questions on file paper. Factorise these expressions:

1.	(a) $x^2 - 25$	(b) y ² - 49	(c) $w^2 - 100$	(d) $x^2 - 4$
	(e) $c^2 - 64$	(f) $x^2 - 1$	(g) $x^2 - 900$	(h) y ² - 9
	(i) $16 - x^2$	(j) 1 - y ²	(k) 81 - x ²	(l) $144 - h^2$
	(m) $x^2 - y^2$	(n) $a^2 - c^2$	(o) $9x^2 - 25$	(p) 4y ² – 1
2.	(a) x ⁴ - 1	(b) y ⁴ - 16	(c) a ⁴ – 25	(d) $x^4 - y^4$
	(e) $h^2 - p^4$	(f) $16x^4 - 49$	(g) y ⁶ - 36	(h) x ⁶ - 64
	(i) $81p^4 - x^6$	(j) 144x ⁸ - 1		

3. Factorise a quadratic where $a \neq 1$



Watch clip number #225

Or Corbett Maths #119

Practice Exercise 1.3

Complete these questions on file paper. Factorise these expressions:

1.	(a) $2x^2 + 7x + 5$	(b) $2x^2 + 11x + 15$	(c) $2x^2 + 9x + 10$
	(d) $3x^2 + 13x + 4$	(e) $3x^2 + 4x + 1$	(f) $3x^2 + 8x + 4$
2.	(a) $3x^2 + x - 4$	(b) $7x^2 + 20x - 3$	(c) $2x^2 - 13x + 15$
	(d) $3x^2 - 17x + 10$	(e) $3x^2 - 16x - 12$	(f) $3x^2 - x - 4$
3.	(a) $6x^2 + 13x + 6$	(b) $9x^2 + 9x + 2$	(c) $6x^2 + 13x + 2$
	(d) $8x^2 + 41x + 5$	(e) $9x^2 + 6x + 1$	(f) $8x^2 + 26x + 15$
4.	(a) $9x^2 - 12x - 5$	(b) $4x^2 - 4x - 3$	(c) $4x^2 - 11x + 6$

4. Solve a quadratic equation by factorising



Watch clip number #230

Or Corbett Maths #266

Practice Exercise 1.4

Complete these questions on file paper. Solve these equations by factorising:

1.	(a) $x^2 + 6x + 8 = 0$	(b) $x^2 + 7x + 12 = 0$	(c) $y^2 + 7y + 10 = 0$
	(d) $y^2 + 3y - 4 = 0$	(e) $x^2 - 2x - 8 = 0$	(f) $m^2 - 7m + 12 = 0$
	(g) $y^2 - 10y + 25 = 0$	(h) $y^2 - 4y - 45 = 0$	(i) $x^2 - x - 56 = 0$
2.	(a) $x^2 - 9 = 0$	(b) $y^2 - 100 = 0$	(c) $w^2 - 1 = 0$
	(d) $k^2 - 144 = 0$	(e) $x^2 - 64 = 0$	(f) $c^2 - 0.25 = 0$
3.	(a) $x^2 + 2x = -1$	(b) $y^2 + 8y + 10 = 3$	(c) $x^2 = 7x - 12$
	(d) $y^2 + 6y + 15 = 3 - 7y$	(e) $x^2 - x - 8 = 2x + 2$	(f) $2x^2 - 14x + 49 = x^2$

Mark your work.

5. Write a quadratic in completed square form

k hegartymaths Watch clip number #235-237 Or Corbett Maths #10

Practice Exercise 1.5

Complete these questions on file paper. Write these expressions in completed square form:

1. (a) $x^2 + 8x + 1$ (b) $x^2 + 10x + 3$ (c) $x^2 + 2x - 1$ (d) $x^2 - 6x - 10$ (e) $x^2 - 4x - 13$ (f) $x^2 - 12x + 3$ (g) $x^2 + 14x + 3$ (h) $x^2 - 2x - 15$ (i) $x^2 + 4x - 11$ (j) $x^2 + x - 8$ (k) $x^2 + 3x + 1$ (l) $x^2 - 7x - 2$

2. (a) $2x^2 + 8x + 2$ (b) $2x^2 + 12x - 3$ (c) $3x^2 - 12x + 2$ (d) $4x^2 + 12x - 5$ (e) $2x^2 - 3x - 5$ (f) $5x^2 - 20x + 30$

Mark your work.

6. Solve a quadratic equation by completing the square



Watch clip number #238-239

Or Corbett Maths #267a

Practice Exercise 1.6

Complete these questions on file paper. Solve these equations by completing the square:

1.	(a) $x^2 + 6x + 8 = 0$	(b) $x^2 + 10x + 24 = 0$	(c) $x^2 + 14x + 40 = 0$
	(d) $x^2 - 4x - 45 = 0$	(e) $x^2 - 12x + 35 = 0$	(f) $x^2 - 2x - 3 = 0$
2.	(a) $x^2 + 5x + 4 = 0$	(b) $x^2 - 3x - 18 = 0$	(c) $x^2 + x - 12 = 0$
	(d) $x^2 - 7x + 12 = 0$	(e) $x^2 - 11x + 24 = 0$	(f) $x^2 - 7x - 30 = 0$

3. Write your answers in surd form where appropriate:

(a) $x^2 + 4x - 3 = 0$	(b) $x^2 + 6x - 10 = 0$	(c) $x^2 - 2x - 5 = 0$
(d) $x^2 - 10x + 1 = 0$	(e) $x^2 + 8x + 3 = 0$	(f) $x^2 - 8x - 22 = 0$
(a) $5x^2 + 30x - 10 = 0$	(b) $2x^2 + 7x + 3 = 0$	(c) $3x^2 + 12x - 2 = 0$
(d) $2x^2 - 3x - 7 = 0$	(e) $5x^2 + 2x - 8 = 0$	(f) $10x^2 - 2x - 1 = 0$

Mark your work.

4.



Bridging Unit 2 – Quadratic Graphs

You need to be able to confidently:

- Complete a table of values and plot a quadratic graph
- Sketch a quadratic graph given its equation by
 - Finding the *x*-intercept(s) (if any)
 - Finding the *y*-intercept
 - $_{\odot}~$ Finding the coordinates of the vertex by writing in completed square form
- Write down the equation of a quadratic given the graph

1. Complete a table of values and plot a quadratic graph



Watch clip number #251

Or Corbett Maths #264

Practice Exercise 2.1

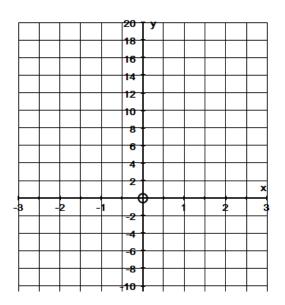
Print out the next page and answer the questions on it.

- If you use a calculator to work out the values, remember that when x is negative you must put brackets around it when you square it, i.e. $(-3)^2$.
- Make sure that you plot and draw the graphs in pencil.
- If your graph is not a smooth U or ∩ shape then at least one of your values must be incorrect or you have plotted something incorrectly, so look for your mistake and correct it.
- Each graph should be symmetrical, but not necessarily in the *y*-axis (and remember that you are only plotting a small section of it).

1.
$$y = x^2 - x^2$$

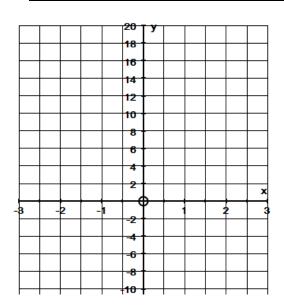
4

x	-3	-2	-1	0	1	2	3
У							



2.	ν	=	x^2	+	2 <i>x</i>
	1				

x	-3	-2	-1	0	1	2	3
У							

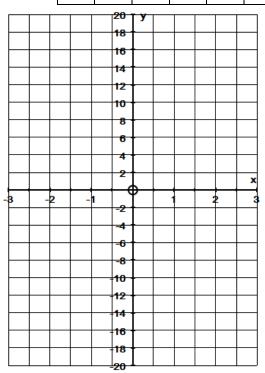


3.
$$y = 5x - x^2$$

JA	л						
x	-3	-2	-1	0	1	2	3
У							
	2				2		
		-4 -6 -10 -12 -14 -14 -16 -18 -20					

4.
$$y = x^2 + 4x + 7$$

x	-3	-2	-1	0	1	2	3
у							



2. Sketch a quadratic graph given its equation

This previous section was about plotting an accurate quadratic curve on numbered coordinate axes. What we are talking about here is *sketching the correct shape* of a quadratic graph, without scales on the axes but *labelling the significant points* with their coordinates (the intercepts and turning point).



Watch clip number #257

Or Corbett Maths #265

Practice Exercise 2.2

Complete these questions on **squared** paper. Draw your graphs in pencil, and axes with a ruler.

For each question show that you have:

- a. Decided whether the graph is U-shaped (if the coefficient of x^2 is positive) or \cap -shaped (if the coefficient of x^2 is negative).
- b. Found the *x*-intercept(s) by setting y = 0 and solving the equation (by any of the methods from Unit 1).
- c. Found the *y*-intercept by setting x = 0.
- d. Found the coordinates of the vertex by writing the equation in completed square form.
- 1. Sketch the graph of $y = x^2 + 10x + 9$
- 2. Sketch the graph of $y = x^2 + 6x + 8$
- 3. Sketch the graph of $y = x^2 2x 3$
- 4. Sketch the graph of $y = -x^2 2x + 8$

3. Write down the equation of a quadratic given the graph



If necessary watch clip number #257 again.

Or Corbett Maths #265

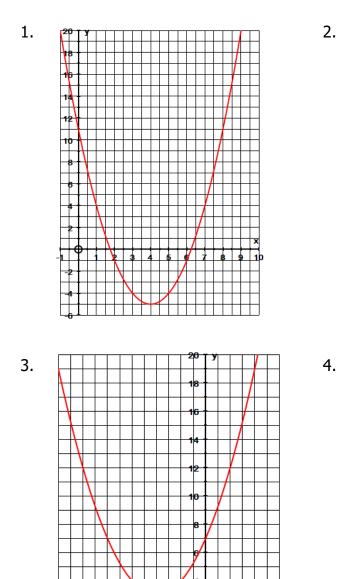
Practice Exercise 2.3

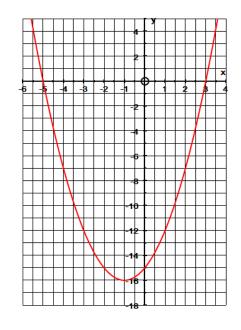
Complete these questions on file paper. Write down the equations of the graphs shown.

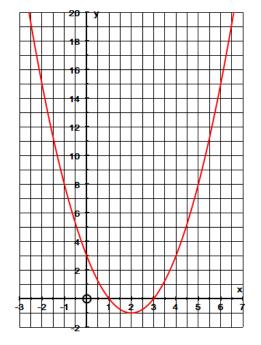
You are now working backwards from what you did before.

- If you know the coordinates of the vertex you can write the equation in completed square form.
- If you know the *x*-intercept(s) you can write the equation in factorised form.

In either case check your answer by expanding and simplifying, then checking that the *y*-intercept is correct.









[©] Bridging Unit 3 – Linear Graphs

You need to be able to confidently:

- Write the equation for/draw a straight line using the gradient and intercept
- Find the gradient and y-intercept of a line by rearranging its equation
- Find the equation of a line using gradient and coordinates
- Find the equation of a perpendicular line

1. Write the equation for/draw a straight line using the gradient and intercept

This unit assumes that you can draw a straight line graph by filling in a table of values and plotting points.



Watch clip number #207-209

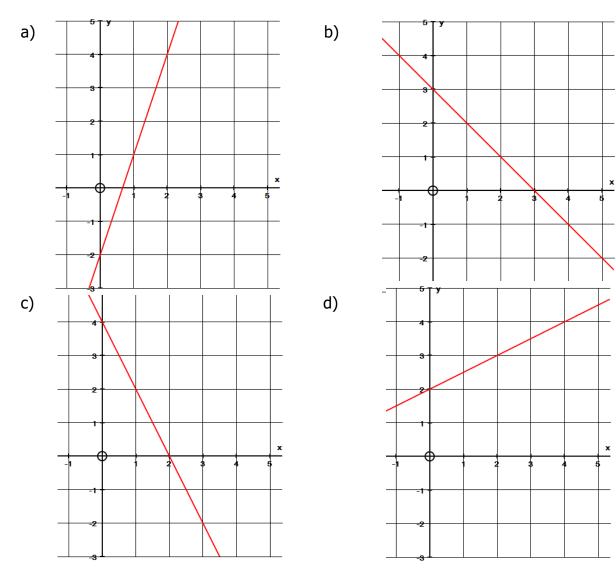
Or Corbett Maths #187

Practice Exercise 3.1

Complete these questions on squared paper.

- 1. Write down the gradient and *y*-intercept of the line with equation:
 - a) y = 7x 8
 - b) y = 2x + 9
 - c) y = 0.5x
- 2. Write down the equation of the line with:
 - a) Gradient 5 and *y*-intercept -2
 - b) Gradient 10 and y-intercept 7
 - c) Gradient -3 and *y*-intercept 1
- 3. On squared paper, draw the graphs from questions 1 and 2. Do <u>not</u> use a table of values; use the gradient and *y*-intercept.

4. Write down the equation of these graphs by identifying the gradient and *y*-intercept:



2. Find the gradient and y-intercept of a line by rearranging its equation



Watch clip number #210

Or Corbett Maths #191

Practice Exercise 3.2

Complete these questions on file paper.

For each question:

- a) Use the balance method (showing all your working) to rearrange these equations into the form y = mx + c
- b) Identify the gradient and *y*-intercept.

1.	x + y = 13	2.	$\frac{y}{2} = 2x + 3$
3.	2x - y = -7	4.	4x + 2y = 5
5.	x = 20 - 4y	6.	6x = 2y + 3
7.	$6x = \frac{y}{3} + 3$	8.	6x = 7(y - 1)
9.	6(x-2) = 5y	10.	6x - 5y = 4

Mark your work.

3. Find the equation of a line using gradient and coordinates



Watch clip number #212

Or Corbett Maths #194

Practice Exercise 3.3

Complete these questions on file paper.

Write down the equation of the graph which:

- 1.
- 3.
- Has gradient 3 and goes through (1, 4). 2. Has gradient 7 and goes through (-2, 7).
- Has gradient -2 and goes through (2, 4). 4. Has gradient -10 and goes through (-3, 5).
- 5. Goes through (0, 4) and (2, 10). 6. Goes through (2, 10) and (4, 14).

- 7. Goes through (-1, -4) and (7, 12). 8. Goes through (3, -7) and (11, -3).
- 9. Is parallel to the line y = 4x + 2 and goes through the point (4, 5).
- 10. Is parallel to the line x + y = 6 and goes through the point (3, -7).
- 11. Is parallel to the line x y = 5 and goes through the point (3, 10).
- 12. Is parallel to the line x 2y = 16 and goes through the point (-4, 5).

Mark your work.

4. Find the equation of a perpendicular line



Watch clip number #216

Or Corbett Maths #197

Practice Exercise 3.4

Complete these questions on file paper.

- 1. Find the equation of the line which is perpendicular to the line y = 2x 8and goes through the point (0, 4).
- 2. Find the equation of the line which is perpendicular to the line y = -3x + 13and goes through the point (1, 2).
- 3. Find the equation of the line which is perpendicular to the line $y = \frac{1}{2}x$ and goes through the point (5, 8).
- 4. Find the equation of the line which is perpendicular to the line $y = \frac{1}{8}x 3$ and goes through the point (-1, 4).
- 5. Find the equation of the line which is perpendicular to the line $y = -\frac{2}{3}x + 23$ and goes through the point (3, -5).



You need to be able to confidently:

- Apply the Index Laws with numbers or algebra
- Work with negative and fractional indices
- Manipulate expressions containing surds (including simplifying surds, expanding brackets containing surds and rationalising a denominator)

1. Apply the Index Laws with numbers or algebra



Watch clip number #110

Or Corbett Maths #174

Practice Exercise 4.1a

Complete these questions on file paper. Do not use a calculator.

1	Write as a power of a $2^4 \times 2^5$		c $2^2 \times 2^6$	d $2^4 \times 2^3$	e $2^4 \times 2^6$
2	Write as a power of a $3^4 \div 3^2$	b $3^5 \div 3^2$	c 3 ⁴ ÷ 3	d $3^6 \div 3^2$	e $3^{10} \div 3^4$
3	Write as a power of a $4^4 \div 4^2$	of a single number b $5^7 \div 5^2$	c $3^4 \times 3^2$	d $6^4 \times 6^3$	e $10^4 \div 10^2$
4	Find the value of n a $3^n \div 3^2 = 3^3$	b $8^5 \div 8^n = 8^2$	c $2^5 \times 2^n = 2^{10}$	d $3^n \times 3^5 = 3^9$	e $2^6 \times 2^3 = 2^n$
5	Work out a $3^4 \div 3^2$	b $4^5 \div 4^3$	c $2^5 \div 2^2$	d $10^4 \times 10^2$	e $6^5 \div 6^5$
6	Write as a power a $\frac{3^3 \times 3^5}{3^4}$	of 3 b (3 ³) ²	c $\frac{3 \times 3^7}{3^4}$	d $\frac{3^9}{3^4 \times 3^3}$	e $\frac{3^2 \times 3^{10}}{3^2 \times 3^5}$
7	Write as a power a $\frac{2^3 \times 2^4}{2^5}$	of a single number b $\frac{3^4 \times 3^3}{3^4}$	c $\frac{5^3 \times 5^5}{5^6}$	d $\frac{10^8 \times 10^3}{10^7}$	$e \frac{4^5 \times 4}{4^2}$

8	Work out a $\frac{5^5}{5^2 \times 5^2}$	b $\frac{3^4}{3^2 \times 3^2}$	c $\frac{4^7}{4^2 \times 4^3}$	d $\frac{2^3 \times 2^4}{2^4 \times 2^2}$	$e \ \frac{3 \times 3^7}{3^4 \times 3^2}$
9	Work out the value a $40 = 5 \times 2^n$	b $32 = 2^n$	ng. c $50 = 5^n \times 2$	d $48 = 3 \times 2^n$	e 54= 2 × 3 ^{<i>n</i>}

Mark your work.

Practice Exercise 4.1b

Complete these questions on file paper.

1	Simplify				
	a $x^3 \times x^2$	b $y^5 \times y^3$	c $n \times n^6$	d $q^7 imes q$	e $x^5 \div x^3$
	f $y^7 \div y^3$	g $p^5 \div p^4$	h $q^7 \div q$	i $y \times y^4 \times y^3$	$\mathbf{j} q^{4} \times q \div q^{3}$
2	Simplify				
	a $3x^2 \times x^5$	b $4p \times 2p$	4	c $4p \times 5p$	d $2 \times 2r^8 \times 4r$
	e $6y^6 \div 2y^3$	f $12q^2 \div 6$	5q	g $8x^9 \div 2x^8$	h $4q \div 2q$
	i $2y^2 \times 3y^3 \times y^3$	$j 6q \times 5q$	$^{4}\div 2q^{5}$		
3	Simplify				
	a i $x^2 \times x$	ii $x^5 \div x^2$		$iii (x^2 \times x) + (x^5 \div x^2)$	
	b $(8y^6 \div 2y^2) - ($	$(2y^2 \times y^2)$			
4	Simplify				
	a $3a^4 \times a^3b^2$	b 2 <i>ab</i>	$a^4 \times 4a^3b$	c 5p ⁴ q ³ >	$\langle 2q^{3}p^{2}$
	d $18x^8y^6 \div 6x^3y^6$	² e 12 <i>a</i>	$a^3b^5 \div 3a^3b$	f 20 <i>p</i> ⁴ <i>q</i> -	$\div 2p^3q^2$
5	Find the value of				
	a 4 <i>x</i> ⁰	b (<i>xy</i>)	0		
6	Write as a power o	f x			
	a $\frac{1}{x^4}$	b $\frac{1}{-}$	c $\frac{1}{1}$	d $\frac{1}{x^4 \div x}$	$e \frac{1}{5 \cdot 7}$
7		X	$x^{4} \times x^{3}$	$x^{\star} \div x$	$x^3 \div x^r$
1	Simplify $(x^{5})^{3}$	b $(2y^2)^4$	$a^{(a2b4)5}$	$d(2a^{3}b)^{3}$	
	a $(x^5)^3$ e $(x^2)^{-1}$			d $(3a^{3}b)^{3}$ h $(-2b^{-4})^{-2} \div$	$-h^2$
~		• (5 (<i>cr</i> /		0
8	Simplify $(r^2)^0$	b (y ⁰) ⁴	$(2a^{3}b^{-2})^{-1}$	$^{-3} \times (2a^{-3}b)^{3}$	
	a $(x^2)^0$		c (2 <i>u v</i>)	$\wedge (2u b)$	

2. Work with negative and fractional indices

If necessary watch clip number #110 again

Or Corbett Maths #173 & #175

Practice Exercise 4.2a

Complete these questions on file paper. Do not use a calculator.

1	Work out the valu	e of the following.			
	a 2 ⁻¹	b 3 ⁻²	c 5 ⁻¹	d 10 ⁻³	e 2 ⁰
	f 2.5 ⁻¹	g $\left(\frac{1}{3}\right)^{-1}$	$h\left(\frac{2}{3}\right)^{-2}$		
2	Simplify the follow a $3^2 \times 3^{-3}$	-	c $5^4 \times 5^{-2}$	d $6^2 \times 6^{-4}$	e $2^2 \times 2^{-5}$
3	Simplify the follow a $4^{-2} \div 4^{-1}$		c $2^{-2} \div 2^{-4}$	d $10^{-4} \div 10^{-3}$	e $5^{-3} \div 5^{-1}$
4	Simplify the follow a $\frac{2^4 \times 2^2}{2^7}$	-	$c \frac{5^{-2} \times 5^2}{5}$	d $\frac{4^{-3} \times 4^{3}}{4^{-2}}$	$e \frac{2^{-4} \times 2^2}{2^{-7}}$
5	Simplify the follow a $\frac{2^4}{2^7 \times 2^{-2}}$	-	c $\frac{5^4 \times 5^{-2}}{5^2 \times 5^{-1}}$	d $\frac{4^4 \times 4^{-2}}{4^{-1}}$	$e \ \frac{2^4 \times 2^2}{2^7 \times 2^{-1}}$
6		\imath in each of the follo	owing.	F 2	12

a
$$2^n = \frac{2^2}{2^5}$$
 b $3 \times 3^n = \frac{3^3}{3^5}$ **c** $\frac{5^n}{5} = \frac{5^2}{5^5}$ **d** $4^2 \times 4^n = \frac{4^2}{4^6}$

Practice Exercise 4.2b

Complete these questions on file paper. Do not use a calculator.

1	Work out the value	e of			1
	a 9 ^{1/2}	b $25^{\frac{1}{2}}$	c $100^{\frac{1}{2}}$	d $4^{\frac{1}{2}}$	$\left(\frac{1}{4}\right)^{\frac{1}{2}}$
2	Work out the value	e of			1
	a 27 ^{¹/₃}	b $1000^{\frac{1}{3}}$	c $-64^{\frac{1}{3}}$	d $125^{\frac{1}{3}}$	e $\left(\frac{1}{125}\right)^{\frac{1}{3}}$
3	Work out as a sing	gle fraction the valu	ue of		
	a $\left(\frac{1}{2}\right)^4$	b $\left(\frac{1}{3}\right)^2$	$\left(\frac{2}{3}\right)^2$	d $\left(\frac{2}{5}\right)^2$	$e \left(\frac{3}{4}\right)^3$
4	Work out the valu	e of			
	a $27^{\frac{2}{3}}$	b 1000 ^{2/3}	c $64^{\frac{2}{3}}$	d 16 ³ / ₄	e $25^{\frac{3}{2}}$
5	Work out as a sing	gle fraction the valu	ue of		
	a 25 ^{-1/2}	b $9^{-\frac{1}{2}}$	c $27^{-\frac{1}{3}}$	d $8^{-\frac{2}{3}}$	e $64^{-\frac{3}{2}}$
6	Find the value of <i>n</i>				
	a $\frac{1}{\sqrt{5}} = 5^n$	b $(\sqrt{7})^5 = 7$	n	c $(\sqrt[3]{2})^{11} = 2^n$	

3. Manipulate expressions containing surds

(including simplifying surds, expanding brackets containing surds and rationalising a denominator)



Watch clip numbers #115, #117-119

Or Corbett Maths #308 & #307

Practice Exercise 4.3

Complete these questions on file paper.

1 Find the value of the integer k.

a $\sqrt{8} = k\sqrt{2}$ **b** $\sqrt{18} = k\sqrt{2}$ **c** $\sqrt{50} = k\sqrt{2}$ **d** $\sqrt{80} = k\sqrt{5}$ **e** $\sqrt{72} = k\sqrt{2}$

2 Expand these expressions. Write your answers in the form $a + b\sqrt{c}$ where a, b and c are integers.

- a $\sqrt{3}(2+\sqrt{3})$ b $(\sqrt{3}+1)(2+\sqrt{3})$ c $(\sqrt{5}-1)(2+\sqrt{5})$ d $(\sqrt{7}+1)(2-2\sqrt{7})$ e $(2-\sqrt{3})^2$
- 3 Rationalise the denominators.
 - **a** $\frac{1}{\sqrt{2}}$ **b** $\frac{1}{\sqrt{5}}$ **c** $\frac{2}{\sqrt{7}}$ **d** $\frac{3}{\sqrt{2}}$ **e** $\frac{5}{\sqrt{11}}$
- 4 Rationalise the denominators and simplify your answers.
 - **a** $\frac{2}{\sqrt{6}}$ **b** $\frac{3}{\sqrt{12}}$ **c** $\frac{5}{\sqrt{10}}$ **d** $\frac{2}{\sqrt{2}}$ **e** $\frac{10}{\sqrt{5}}$
- **5** Rationalise the denominators and give your answers in the form $a + b\sqrt{c}$ where a, b and c are integers.
 - **a** $\frac{2+\sqrt{2}}{\sqrt{2}}$ **b** $\frac{2-\sqrt{2}}{\sqrt{2}}$ **c** $\frac{10+\sqrt{5}}{\sqrt{5}}$ **d** $\frac{5-\sqrt{5}}{\sqrt{5}}$ **e** $\frac{14+\sqrt{7}}{\sqrt{7}}$
- 6 The lengths of the two shorter sides of a right-angled triangle are $\sqrt{7}$ cm and 3 cm. Find the length of the hypotenuse.
- 7 The length of the side of a square is $(1 + \sqrt{2})$ cm. Work out the area of the square. Give your answer in the form $(a + b\sqrt{2})$ cm² where a and b are integers.
- 8 The length of a rectangle is $(3 + \sqrt{5})$ cm. The width of the rectangle is $(4 \sqrt{5})$ cm.

Work out **a** the perimeter of the rectangle **b** the area of the rectangle.



You need to be able to confidently:

- Solve linear simultaneous equations by elimination
- Solve linear simultaneous equations by substitution
- Solve simultaneous equations where one is linear and one quadratic or a circle
- Solve simultaneous equations graphically

1. Solve linear simultaneous equations by elimination



Watch clip number #192-193

Or Corbett Maths #295

Practice Exercise 5.1

Complete these questions on file paper.

1.	(a)		x + y = 18 x + y = 14	(b)		x + 2y = 10 + 2y = 7	(c)		9x - 4y = 19 4x + 4y = 20
	(d)		x + y = 36 - y = 9	(e)		x - 3y = 12 x - 3y = 2	(f)		3x – 6y = 6 2x – 6y = 3
2.	(a	ı)	3x + 2y = 23 2x - y = 6	(1	b)	3x - 3y = 9 $2x + y = 12$		(c)	4x + 2y = 34 3x + y = 21
	(d	1)	9x - 4y = 59 $2x - y = 12$	(6	e)	2x + 8y = 43 x + 3y = 18		(f)	6x + 3y = 45 2x - 2y = 12
3.	(a)		x + 2y = 14 x - 3y = 19	(b)		x + 3y = 1 x + 2y = -22	(c)		5x + 3y = 22 2x + 4y = 20

(d) 5x - 6y = 284x - 4y = 24 (e) 3x + 2y = 72x + 9y = 43 (f) 3x + 3y = -64x - 4y = -24

2. Solve linear simultaneous equations by substitution



Watch clip number #194.

Or Corbett Maths #296 & #298

Practice Exercise 5.2

Complete these questions on file paper.

- 1. (a) y = x + 3 $y = x^{2} + 5x - 2$ (b) $y = x^{2} + x - 14$ y = x - 5 (c) y = 2x - 1 $y = x^{2} - 2x + 2$
 - (d) $y = 2x^2 + 9x + 1$ y = 3x + 9(e) $y = 2x^2 + x + 1$ $y = x^2 - 5x - 7$ (f) $y = -x^2 + 5x + 2$ $y = 3x^2 - x - 2$
- 2. (a) x + y = 4 $y = x^2 + 3x - 1$ (b) x + y = 7xy = 10 (c) $x^2 + y^2 = 13$ x + y = 5
 - (d) 2x y + 4 = 0 $y = x^2 + x - 2$ (e) $x^2 + y^2 = 29$ 7 + x + y = 0(f) xy = -6x + 2y = -4
- 3. (a) 2x + y = 7 $x^2 - y^2 = 8$ (b) $x^2 + y^2 = 20$ y = x + 3 (c) $y = x^2 - 9x - 3$ y = x
 - (d) $2x^2 + y^2 = 10$ 2x - y = 5 (e) $y = x^2 + x - 7$ 4x + 2y + 1 = 0 (f) y = x - 2 $2x^2 - xy = 11$

3. Solve simultaneous equations where one is linear and one quadratic or a circle



Watch clip number #246

Or Corbett Maths #298

Practice Exercise 5.3

Complete these questions on file paper.

- **1** Solve these simultaneous equations.
 - **a** y = 2x and $y = 2x^2$

c
$$y = 3x - 1$$
 and $y = x^2 - 5$

- 2 Solve
 - **a** y 3x = 4 and $y = 2x^2 5$
 - **c** y + 2x = 5 and $y = 2x^2 + x$
 - **e** 2x y = -8 and $y = x^2$

- **b** y = x + 3 and $y = x^2 + 3x$ **d** $y = 6 - x^2$ and y = 4x + 1
- **b** x + y = 2 and $y = 3x^2 2$ **d** x - y = 3 and $y = x^2 - 2x - 1$
- **f** 2x + 3y = 13 and $y = x^2 1$

4. Solve simultaneous equations graphically



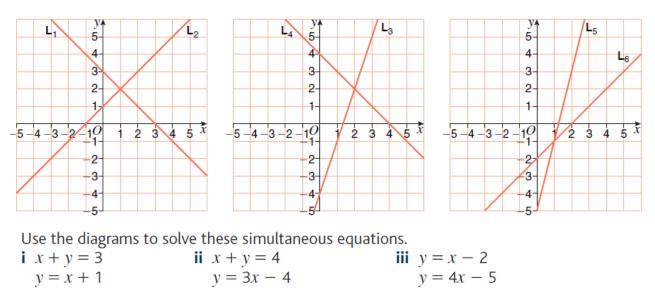
Watch clip number #218-219 & #259

Or Corbett Maths #297

Practice Exercise 5.4

Complete these questions on squared paper.

1. The diagrams show six lines labelled L₁, L₂, L₃, L₄, L₅ and L₆.



Solve these simultaneous equations by drawing both graphs on one set of axes (from -5 to 5) and finding the point of intersection:

2 x + y = 0 y = x + 2 **3** y = x - 2 y = 2x **4** x + y = 1 **5** y = x + 1 **6** y = 2x - 5y = -2x - 1 **7** y = 2x + 4 **8** x + y = 4

Solve these simultaneous equations by drawing both graphs on one set of axes and finding the points of intersection, remembering to pair up the values correctly:

- 7. **a** y = 3 and $y = x^2 + 2x$ **c** y = -4 and $y = x^2 - 5x$
- 8. **a** y = x + 6 and $y = x^2$
 - **c** y = x + 1 and $y = 2x^2$
 - **e** y = x and $y = x^2 + 7x + 5$

- **b** y = 5 and $y = x^2 4x$
- **d** y = -1 and $y = 2x^2 + 5x + 1$
- **b** y = x and $y = x^2 2$
- **d** y = 4 x and $y = 2x^2 + 3$
- **f** x + 2y = 0 and $y = 2x^2 4x 1$



You need to be able to confidently:

- Solve linear inequalities
- Solve quadratic inequalities
- Plot a region using inequalities on a graph

1. Solve linear inequalities

Watch clip number #169-172



Or Corbett Maths #178-179

Practice Exercise 6.1

Complete these questions on file paper. Solve each of the inequalities below:

1.	(a)	$2x + 1 \le 9$ (b) $3x - 5 > 16$ (c) $4x + 8 < 32$ (d) $5x - 2 \ge 68$
	(e)	$\frac{x}{2} + 1 \le 5$ (f) $\frac{x}{9} - 6 > 4$ (g) $\frac{x+3}{2} \ge 5$ (h) $\frac{x-5}{4} > 2$
2.	(a)	$5(x-3) \ge 40$ (b) $6(x+2) < 42$ (c) $2(5x+1) \le 36$
	(d)	$4(x-2) < 18$ (e) $2(2x-9) \ge 22$ (f) $3(2x+7) \le 9$
3	(2)	$4x + 3 > 2x + 11$ (b) $x + 1 \ge 3x - 18$
5.	(a)	$4x + 3 > 2x + 11$ (b) $x + 1 \ge 3x - 18$
	(c)	$13x - 12 < 3x + 13$ (d) $7x - 5 \ge 3x + 11$
4.	(a)	$6 < x + 3 < 10$ (b) $4 \le 2x \le 7$ (c) $1 \le 3x < 9$
	(d)	$4 < \frac{x}{5} < 6$ (e) $9 \le 2x + 3 \le 25$ (f) $-3 \le \frac{x}{4} - 1 < 0$

2. Solve quadratic inequalities

A hegartymaths

Watch clip number #277

Or Corbett Maths #378

Practice Exercise 6.2

Complete these questions on file paper. Solve the following inequalities:

1.	(a)	(x-4)(x-1) < 0	(b) $(x-2)(x+1) < 0$	(c)	$(x + 7)(x + 3) \le 0$
	(d)	$(x-5)(x+4) \leq 0$	((e) $x(x-9) > 0$	(f)	(x+6)(x-5) > 0
	(g)	$(x+10)(x+1)\geq 0$	(h) $(x-7)(x+7) \ge 0$	(i)	(x + 8)(x + 2) < 0
(a) x	$^{2} + 5x + 6 > 0$	(b)	$x^2 + 7x + 10 < 0$	(c) x	$x^2 - 4x - 5 \le 0$
(d) x ²	$^{2} + 2x - 24 > 0$	(e)	$x^2 - 6x + 8 \ge 0$	(f) x	$^{2} + 3x - 4 < 0$

(g)	(g) $x^2 - x - 56 > 0$ (h)		+ 18 < 0	(i) $x^2 - 13x + 22 \le 0$
с	(a) $x^4 - 1$	(b) $v^4 - 16$	(c) $a^4 - 25$	(d) $x^4 - y^4$

2.	(a) x ⁴ – 1	(b) y ⁴ – 16	(c) a ⁴ – 25	(d) $x^4 - y^4$

(e) $h^2 - p^4$	(f) $16x^4 - 49$	(g) y ⁶ – 36	(h) x ⁶ - 64
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(i)	81p ⁴ – x ⁶	(j) 144x ⁸ – 1
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3. Factorise a quadratic where $a \neq 1$



Watch clip number #225

Or Corbett Maths #119

Practice Exercise 1.3

Complete these questions on file paper. Factorise these expressions:

1.	(a) $2x^2 + 7x + 5$	(b) $2x^2 + 11x + 15$	(c) $2x^2 + 9x + 10$
	(d) $3x^2 + 13x + 4$	(e) $3x^2 + 4x + 1$	(f) $3x^2 + 8x + 4$
2.	(a) $3x^2 + x - 4$	(b) $7x^2 + 20x - 3$	(c) $2x^2 - 13x + 15$
	(d) $3x^2 - 17x + 10$	(e) $3x^2 - 16x - 12$	(f) $3x^2 - x - 4$
3.	(a) $6x^2 + 13x + 6$	(b) $9x^2 + 9x + 2$	(c) $6x^2 + 13x + 2$
	(d) $8x^2 + 41x + 5$	(e) $9x^2 + 6x + 1$	(f) $8x^2 + 26x + 15$
4.	(a) $9x^2 - 12x - 5$	(b) $4x^2 - 4x - 3$	(c) $4x^2 - 11x + 6$



You need to be able to confidently:

- Find sides and angles in triangles using SOHCAHTOA in 2d and 3d
- Find angles, sides and areas in triangles using the Sine, Cosine and Area rules

1. Find sides and angles in triangles using SOHCAHTOA in 2d and 3d



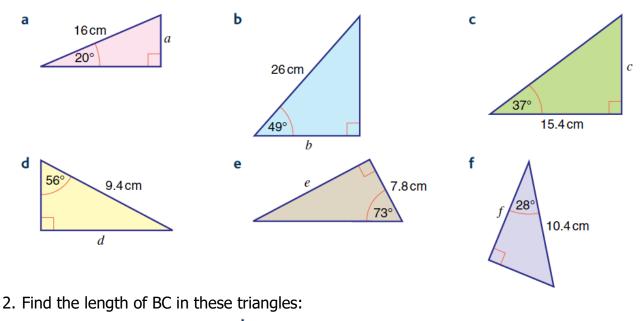
Watch clip number #509 & #511

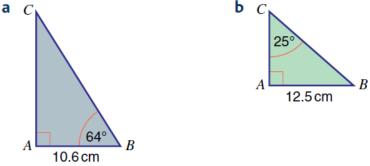
Or Corbett Maths #330-332

Practice Exercise 5.1

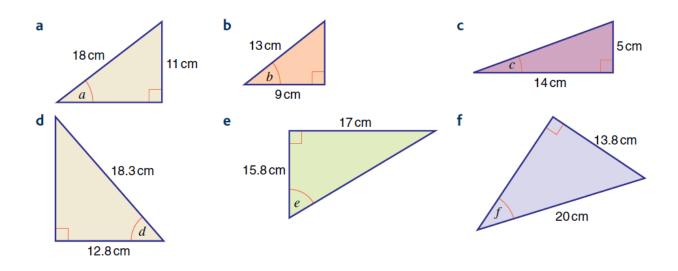
Complete these questions on file paper.

1. Find the lengths of the lettered sides in these triangles:





3. Find the marked angle in these triangles:



- 4. The diagram shows a square-based pyramid. The lengths of sides of the square base, *ABCD*, are 10 cm and the base is on a horizontal plane. The centre of the base is the point *M* and the vertex of the pyramid is *O*, so that *OM* is vertical. The point *E* is the midpoint of the side *AB*.
 - OA = OB = OC = OD = 15 cm.
 - a Calculate the length of i AC ii AM.
 - **b** Calculate the length of *OM*.
 - c Calculate the size of angle OAM.
 - **d** Hence find the size of angle AOC.
 - e Calculate the length of OE.
 - f Calculate the size of angle OAB.

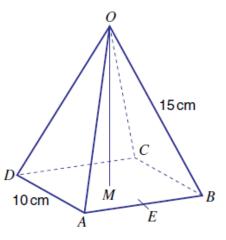
5. *ABCD* is a horizontal rectangular lawn in a garden and *TC* is a vertical pole. Ropes run from the top of the pole, *T*, to the corners, *A*, *B* and *D*, of the lawn.

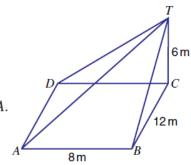
- **a** Calculate the length of the rope *TA*.
- **b** Calculate the size of the angle made with the lawn by

ii the rope *TD*

i the rope TB

iii the rope TA.





2. Find angles, sides and areas in triangles using the Sine, Cosine and Area rules



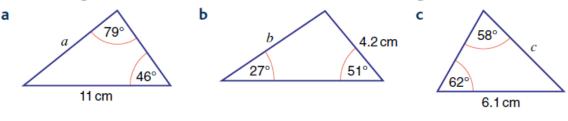
Watch clip number #516, #521, #523, #527, #529

Or Corbett Maths #333-337

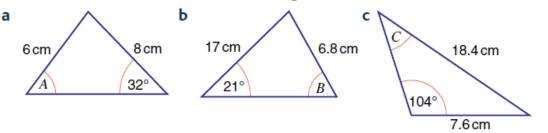
Practice Exercise 5.2

Complete these questions on file paper.

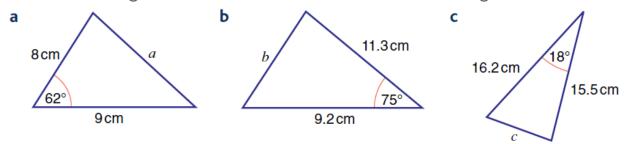
1. Find the lengths of the sides marked with letters in these triangles.



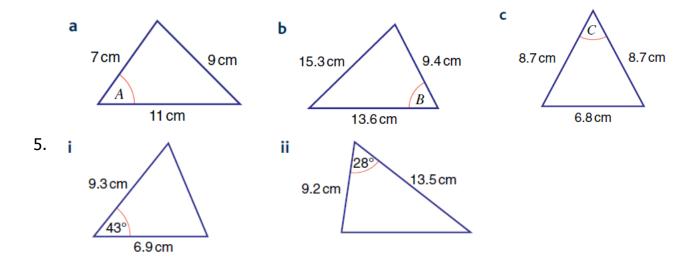
2. Calculate the size of each of the *acute* angles marked with a letter.



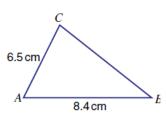
3. Calculate the length of the sides marked with letters in these triangles.



4. Calculate the size of each of the angles marked with a letter in these triangles.



6. The area of triangle ABC is 15 cm²
Angle A is acute.
Work out the size of angle A.

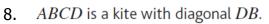


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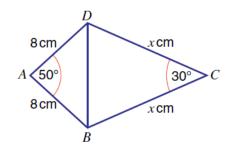
12.6 m

A

7. The area of triangle ABC is 60.7 m² Work out the length of BC.



- **a** Calculate the length of *DB*.
- **b** Calculate the size of angle *BDC*.
- **c** Calculate the value of *x*.
- **d** Calculate the length of *AC*.



В

Unit 1 - Answers

Practice Exercise 1.1

1.	-	(x+3)(x+4) $(x+2)^2$	-	(x + 4)(x + 2) (x + 3)(x + 5)	-	(x+3)(x+2) $(x+3)^2$	-	(x + 7)(x + 1) (x + 7)(x + 4)
2.	-	(x+4)(x-3) (x+8)(x-6)	-	(x+6)(x-1) (x+8)(x-4)	-	(x+5)(x-2) (x+7)(x-5)	-	(x+4)(x-1) (x+11)(x-3)
3.		(x-5)(x+2) (x-4)(x+3)	-	(x-5)(x+4) (x-6)(x+2)	-	(x-9)(x+3) (x-7)(x+3)	-	(x-3)(x+1) (x-11)(x+5)
4.	-	$(x-3)^2$ (x-8)(x-1)	-	(x-5)(x-4) (x-8)(x-4)	-	(x-7)(x-2) (x-7)(x+2)	-	(x-11)(x-2) (x-6)(x-8)
	-	(x-8)(x-1) $(x+6)^2$		(x + 23)(x + 1) (x - 9)(x + 7)	-	(x - 7)(x + 2) (x + 13)(x + 2)	-	(x-3)(x-4) (x+12)(x+5)

Practice Exercise 1.2

1. a)
$$(x + 5)(x - 5)$$
 b) $(y + 7)(y - 7)$
e) $(c + 8)(c - 8)$ f) $(x + 1)(x - 1)$
i) $(16 + x)(16 - x)$ j) $(1 + y)(1 - y)$
m) $(x + y)(x - y)$ n) $(a + c)(a - c)$ c) $(w + 10)(w - 10)$ d) $(x + 2)(x - 2)$
g) $(x + 30)(x - 30)$ h) $(y + 3)(y - 3)$
k) $(9 + x)(9 - x)$ l) $(12 + h)(12 - h)$
o) $(3x + 5)(3x - 5)$ p) $(2x + 1)(2x - 1)$
2. a) $(x^2 + 1)(x^2 - 1)$ b) $(x^2 + 1)(x^2 - 1)$
c) $(a^2 + 5)(a^2 - 5)$ d) $(x^2 + a^2)(x^2 - a^2)$

2. a)
$$(x^2 + 1)(x^2 - 1)$$
 b) $(x^2 + 1)(x^2 - 1)$ c) $(a^2 + 5)(a^2 - 5)$ d) $(x^2 + y^2)(x^2 - y^2)$
e) $(h + p^2)(h - p^2)$ f) $(4x^2 + 7)(4x^2 - 7)$ g) $(y^3 + 6)(y^3 - 6)$ h) $(x^3 + 8)(x^3 - 8)$
i) $(9p^2 + x^3)(9p^2 - x^3)$ j) $(12x^4 + 1)(12x^4 - 1)$

Practice Exercise 1.3

1.	a)	(2x + 5)(x + 1)	b)	(2x+5)(x+3)	c)	(2x + 5)(x + 2)
	d)	(3x + 1)(x + 4)	e)	(3x+1)(x+1)	f)	(3x + 2)(x + 2)
2.	a)	(3x+4)(x-1)	b)	(7x-1)(x+3)	c)	(2x-3)(x-5)
	d)	(3x-2)(x-5)	e)	(3x+2)(x-6)	f)	(3x-4)(x+1)
3.	a)	(3x + 2)(2x + 3)	b)	(3x+2)(3x+1)	c)	(6x + 1)(x + 2)
	d)	(8x + 1)(x + 5)	e)	$(3x+1)^2$	f)	(4x + 3)(2x + 5)
4.	a)	(3x + 1)(3x - 5)	b)	(2x+1)(2x-3)	c)	(4x-3)(x-2)
	d)	(2x - 1)(3x - 2)	e)	(10x-1)(x-9)	f)	(4x-7)(x+8)

Practice Exercise 1.4

1.	d)	x = -4 or x = -2 x = -4 or x = 1 x = 5	e)	x = -4 or $x = -3x = -2$ or $x = 4x = -5$ or $x = 9$	f)	
			•			$\begin{array}{l} x = \pm 1 \\ x = \pm 0.5 \end{array}$
3.	•	x = -1 x = -12 or $x = -1$	•		•	x = 3 or x = 4 x = 7

Practice Exercise 1.5

1.	a)	$(x+4)^2 - 15$	b)	$(x+5)^2 - 22$	c)	$(x+1)^2 - 2$
	d)	$(x-3)^2 - 19$	e)	$(x-2)^2 - 17$	f)	$(x-6)^2 - 33$
	g)	$(x+7)^2 - 46$	h)	$(x-1)^2 - 16$	i)	$(x+2)^2 - 15$
	j)	$(x+\frac{1}{2})^2-\frac{35}{4}$	k)	$(x+\frac{3}{2})^2-\frac{5}{4}$	l)	$(x-\frac{7}{2})^2-\frac{57}{4}$
2.	a)	$2(x+4)^2 - 30$	b)	$2(x+3)^2 - 21$	c)	$3(x-2)^2 - 10$
	d)	$4(x+\frac{3}{2})^2-14$	e)	$2(x-\frac{3}{4})^2-\frac{49}{8}$	f)	$5(x-2)^2 + 10$

Practice Exercise 1.6

1.	a) d)	x = -4 or $x = -2x = -5$ or $x = 9$	•		c) f)	x = -10 or $x = -4x = 3$ or $x = -1$
2.	a) d)	x = -4 or x = -1 x = 3 or x = 4			c) f)	x = -4 or $x = 3x = -3$ or $x = 10$
3.	a)	$(x + 2)^{2} - 7 = 0$ (x + 2) ² = 7 x + 2 = $\pm \sqrt{7}$ x = -2 $\pm \sqrt{7}$	b)	$(x + 3)^{2} - 19 = 0$ (x + 3) ² = 19 x + 3 = $\pm \sqrt{19}$ x = -3 $\pm \sqrt{19}$		$(x-1)^{2} - 6 = 0$ (x-1)^{2} = 6 x-1 = $\pm \sqrt{6}$ x = 1 $\pm \sqrt{6}$
	d)	$(x-5)^{2} - 24 = 0$ (x-5) ² = 24 x-5 = $\pm \sqrt{24}$ x = 5 $\pm \sqrt{24}$	e)	$(x + 4)^{2} - 13 = 0$ (x + 4) ² = 13 x + 4 = ±\sqrt{13} x = -4 ± \sqrt{13}	•	$(x-4)^{2} - 38 = 0$ (x-4)^{2} = 38 x-4 = \pm\sqrt{38} x = 4 ± \sqrt{38}

4. a)
$$5(x^2 + 6x) - 10 = 0$$
 b) $2\left(x^2 + \frac{7}{2}x\right) + 3 = 0$ c) $3(x^2 + 4x) - 2 = 0$
 $5(x + 3)^2 - 55 = 0$ $2(x + \frac{7}{4})^2 - \frac{25}{8} = 0$ $3(x + 2)^2 - 14 = 0$
 $5(x + 3)^2 = 55$ $2(x + \frac{7}{4})^2 = \frac{25}{8}$ $3(x + 2)^2 = 14$
 $(x + 3)^2 = 1$ $(x + \frac{7}{4})^2 = \frac{25}{16}$ $(x + 2)^2 = \frac{14}{3}$
 $x + 3 = \pm\sqrt{1}$ $x + \frac{7}{4} = \pm\sqrt{\frac{25}{16}}$ $x + 2 = \pm\sqrt{\frac{14}{3}}$
 $x = -4 \text{ or } x = -2$ $x = -\frac{1}{4} \text{ or } x = -\frac{11}{4}$ $x = -2 \pm \sqrt{\frac{14}{3}}$

d)
$$2\left(x^2 - \frac{3}{2}x\right) - 7 = 0$$
 e)
 $2\left(x - \frac{3}{4}\right)^2 - \frac{65}{8} = 0$
 $2\left(x - \frac{3}{4}\right)^2 = \frac{65}{8}$
 $\left(x - \frac{3}{4}\right)^2 = \frac{65}{16}$
 $x - \frac{3}{4} = \pm\sqrt{\frac{65}{16}}$
 $x = \frac{3\pm\sqrt{65}}{4}$

$$x = -\frac{1}{4} \text{ or } x = -\frac{1}{4} \qquad x = -2 \pm \sqrt{\frac{1}{3}}$$

$$5 \left(x^2 + \frac{2}{5}x\right) - 8 = 0 \qquad \text{f)} \qquad 10 \left(x^2 - \frac{1}{5}x\right) - 1 = 0$$

$$5 \left(x + \frac{1}{5}\right)^2 - \frac{41}{5} = 0 \qquad 10 \left(x - \frac{1}{10}\right)^2 - \frac{11}{10} = 0$$

$$5 \left(x + \frac{1}{5}\right)^2 = \frac{41}{5} \qquad 10 \left(x - \frac{1}{10}\right)^2 = \frac{11}{10}$$

$$\left(x + \frac{1}{5}\right)^2 = \frac{41}{25} \qquad \left(x - \frac{1}{10}\right)^2 = \frac{11}{100}$$

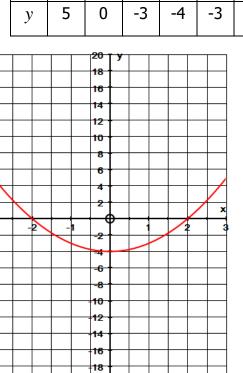
$$x + \frac{1}{5} = \pm \sqrt{\frac{41}{25}} \qquad x - \frac{1}{10} = \pm \sqrt{\frac{11}{100}}$$

$$x = \frac{-1 \pm \sqrt{41}}{25} \qquad x = \frac{1 \pm \sqrt{11}}{100}$$

Unit 2 Answers

Exercise 2.1

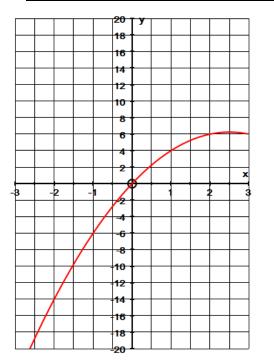
1.
$$y = x^2 - 4$$



20

3. $y = 5x - x^2$

x	-3	-2	-1	0	1	2	З
у	-24	-14	-6	0	4	6	6



$$y = x^2 + 2x$$

2.

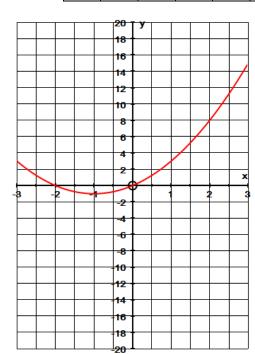
3

5

2

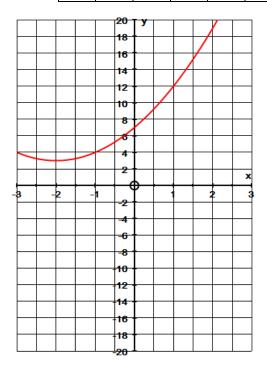
0

x	-3	-2	-1	0	1	2	3
У	3	0	-1	0	3	8	15

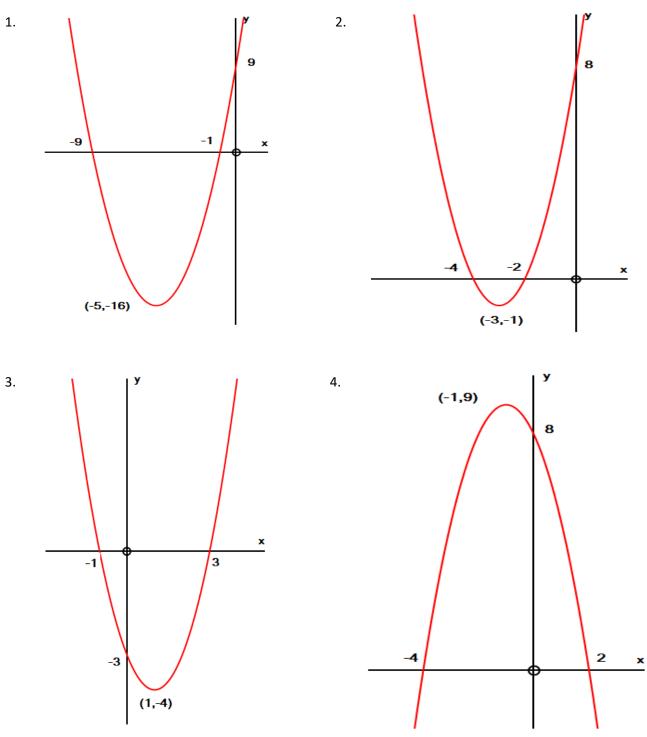


4. $y = x^2 + 4x + 7$

x	-3	-2	-1	0	1	2	3
у	4	3	4	7	12	19	28







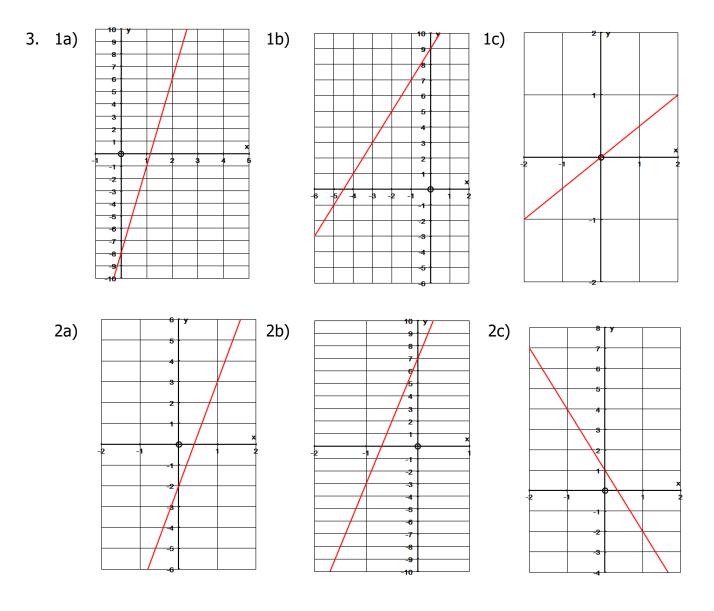
Answers to Exercise 2.3

- 1. $y = (x 4)^2 5$ 2. y = (x 3)(x + 5)3. $y = (x + 2)^2 + 3$ 4. y = (x 1)(x 3)

Unit 3 - Answers

Exercise 3.1

- 1. a) Gradient = 7, y-intercept = -8
 - b) Gradient = 2, y-intercept = 9
 - c) Gradient = 0.5, y-intercept = 0
- 2. a) y = 5x 2b) y = 10x + 7c) y = -3x + 1



- 4. a) y = 3x 2
 - b) y = -x + 3
 - c) y = -2x + 4
 - d) y = 0.5x + 2

Exercise 3.2

1.	y = -x + 13	Gradient = -1,	y-intercept = 13
2.	y = 4x + 6	Gradient = 4,	y-intercept = 6
3.	y = 2x + 7	Gradient = 2,	y-intercept = 7
4.	$y = -2x + \frac{5}{2}$	Gradient = -2,	y-intercept = $\frac{5}{2}$
5.	$y = -\frac{1}{4}x + 5$	Gradient = $-\frac{1}{4'}$	y-intercept = 5
6.	$y = 3x - \frac{3}{2}$	Gradient = 3,	y-intercept = $-\frac{3}{2}$
7.	y = 18x - 9	Gradient = 18,	y-intercept = -9
8.	$y = \frac{6}{7}x + 1$	Gradient = $\frac{6}{7}$,	y-intercept = 1
9.	$y = \frac{6}{5}x - \frac{12}{5}$	Gradient = $\frac{6}{5}$,	y-intercept = $-\frac{12}{5}$
10.	$y = \frac{6}{5}x - \frac{4}{5}$	Gradient = $\frac{6}{5'}$	y-intercept = $-\frac{4}{5}$

Exercise 3.3

1.	y = 3x - 1
2.	y = 7x + 21
3.	y = -2x + 8
4.	y = -10x - 25
5.	y = 3x + 4
6.	y = 2x + 6
7.	y = 2x - 2
8.	$y = \frac{1}{2}x - \frac{17}{2}$
9.	y = 4x - 11
10.	y = -x - 4
11.	y = x + 7
12.	$y = \frac{1}{2}x + 7$

Exercise 3.4

1.	$y = -\frac{1}{2}x + 4$
2.	$y = \frac{1}{3}x + \frac{5}{3}$
3.	y = -2x + 18
4.	y = -8x - 4
5.	$y = \frac{3}{2}x - \frac{19}{2}$

Unit 4 – Answers

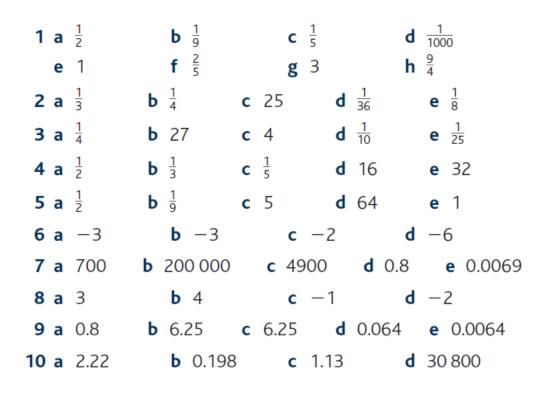
Practice Exercise 4.1a

1 a 2 ⁹	b 2 ⁷	c 2 ⁸	d 2 ⁷	e 2 ¹⁰
2 a 3 ²	b 3 ³	c 3 ³	d 3 ⁴	e 3 ⁶
3 a 4 ²	b 5 ⁵	c 3 ⁶	d 6 ⁷	e 10 ²
4 a 5	b 3	c 5	d 4	e 9
5 a 9	b 16	c 8	d 10 ⁶	e 6
6 a 3 ⁴	b 3 ⁶	c 3 ⁴	d 3 ²	e 3 ⁵
7 a 2 ²	b 3 ³	c 5 ²	d 10 ⁴	e 4 ⁴
8 a 5	b 1	c 16	d 2	e 9
9 a 3	b 5	c 2	d 4	e 3

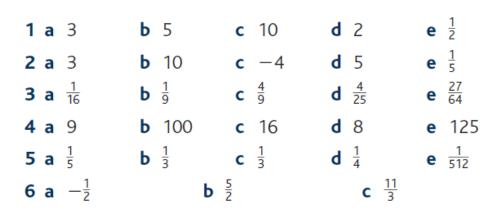
Practice Exercise 4.1b

1 a x ⁵ f y ⁴	b у ⁸ g Р	c n^7 h q^6	d q ⁸ е у і у ⁸ ј q	-
2 a 3 <i>x</i> ⁷ f 2 <i>q</i>	b 8 <i>p</i> ⁵ g 4 <i>x</i>	c 20 <i>p</i> ² h 2	d 16 <i>r</i> ⁹ e 3 i 6 <i>y</i> ⁸ j 1	
3 a i x ³	ii x ³	iii 2 <i>x</i> ³	b 2 <i>y</i> ⁴	
4 a $3a^7b^2$	Ь	$8a^4b^5$	c $10p^6q^6$	
d $3x^5y^4$	е	$4b^{4}$	f 10 pq^{-1}	
5 a 4	Ь	1		
6 a x^{-4}	b x ⁻¹	c x ⁻⁷	d x ⁻³ e x	2
7 a x ¹⁵	b 16y ⁸	c $a^{10}b^{20}$	d $27a^9b^3$	
e x ⁻²	f 16y ⁻⁴	g a^{12}	h $\frac{1}{4}b^{6}$	
8 a 1	b 1	c $a^{-18}b^9$		

Practice Exercise 4.2a



Practice Exercise 4.2b



Practice Exercise 4.3

1a2 b3 c5 d4 e6 **2** a $3 + 2\sqrt{3}$ b $5 + 3\sqrt{3}$ c $3 + \sqrt{5}$ d -12 e $7 - 4\sqrt{3}$ **3** a $\frac{\sqrt{2}}{2}$ b $\frac{\sqrt{5}}{5}$ c $\frac{2\sqrt{7}}{7}$ d $\frac{3\sqrt{2}}{2}$ e $\frac{5\sqrt{11}}{11}$ 4 a $\frac{\sqrt{6}}{3}$ b $\frac{\sqrt{3}}{2}$ c $\frac{\sqrt{10}}{2}$ d $\sqrt{2}$ e $2\sqrt{5}$ **5** a $1 + \sqrt{2}$ b $\sqrt{2} - 1$ c $1 + 2\sqrt{5}$ d $\sqrt{5} - 1$ e $2\sqrt{7} + 1$ 6 4 cm **7** 3 + $2\sqrt{2}$ cm²

8 a i 14 cm ii $7 + \sqrt{5}$ cm²

Unit 5 – Answers

Practice Exercise 5.1

1.	(a) x=2	(b) x=1	(c) x=3
	y=6	y=3	y=2
	(d) x=15	(e) x=5	(f) x=3
	y=6	y=6	y=0.5
2.	(a) x=5	(b) x=5	(c) x=4
	y=4	y=2	y=9
	(d) x=11	(e) x=7.5	(f) x=7
	y=10	y=3.5	y=1
3.	(a) x=5	(b) x= -4	(c) x=2
	y=2	y= 3	y=4
	(d) x=8	(e) x=-1	(f) x=-4
	y=2	y=5	y=2

Practice Exercise 5.2

1.	(a) $x = -5$ and $y = -2$, $x = 1$ and $y = 4$
	(b) $x = -3$ and $y = -8$, $x = 3$ and $y = -2$
	(c) $x = 1$ and $y = 1$, $x = 3$ and $y = 5$
	(d) $x = -4$ and $y = -3$, $x = 1$ and $y = 12$
	(e) $x = -4$ and $y = 29$, $x = -2$ and $y = 7$
	(f) $x = -0.5$ and $y = -0.75$, $x = 2$ and $y = 8$
2.	(a) $x = -5$ and $y = 9$, $x = 1$ and $y = 3$
	(b) $x = 2$ and $y = 5$, $x = 5$ and $y = 2$
	(b) $x = 2$ and $y = 5$, $x = 5$ and $y = 2$ (c) $x = 2$ and $y = 3$, $x = 3$ and $y = 2$
	(c) $x = 2$ and $y = 3$, $x = 3$ and $y = 2$

- 3. (a) x = 3 and y = 1, x = 6.333... and y = -5.666..
 - (b) x = -4.284 and y = -1.284, x = 1.284 and y = 4.284
 - (c) x = -0.2915 and y = -0.2915, x = 10.2915 and y = 10.2915
 - (d) x = 1.14 and y = -2.72, x = 2.19 and y = -0.613
 - (e) x = -4.46 and y = 8.42, x = 1.46 and y = -3.42
 - (f) x = -4.46 and y = -6.46, x = 2.46 and y = 0.46

Practice Exercise 5.3

1 a x = 0, y = 0 or x = 1, y = 2 **b** x = 1, y = 4 or x = -3, y = 0 **c** x = 4, y = 11 or x = -1, y = -4 **d** x = 1, y = 5 or x = -5, y = -9 **2 a** x = 3, y = 13 or x = -1.5, y = -0.5 **b** x = 1, y = 1 or $x = -\frac{4}{3}, y = \frac{10}{3}$ **c** x = 1, y = 3 or $x = -\frac{5}{2}, y = 10$ **d** x = 2, y = -1 or x = 1, y = -2 **e** x = 4, y = 16 or x = -2, y = 4**f** x = 2, y = 3 or $x = -\frac{8}{3}, y = \frac{55}{9}$

Practice Exercise 5.4

1.	i x = 1, y = 2 $ii x = 2, y = 2$	iii $x = 1, y = -1$
2 <i>x</i>	x = -1, y = 1 3 $x = -2, y = -4$ 4	x = -2, y = 3
5 <i>x</i>	= -3, y = -2 6 $x = 3, y = 1$	
7.	a) $x = 1, y = 3$ or $x = -3, y = 3$ c) $x = 1, y = -4$ or $x = 4, y = -4$	b) $x = 5, y = 5$ or $x = -1, y = 5$ d) $x = -2, y = -1$ or $x = -0.5, y = -1$
8.	a) $x = 3, y = 9$ or $x = -2, y = 4$ c) $x = 1, y = 2$ or $x = -0.5, y = 0.5$ e) $x = -1, y = -1$ or $x = -5, y = -5$	b) $x = 2, y = 2$ or $x = -1, y = -1$ d) $x = -1, y = 5$ or $x = 0.5, y = 3.5$ f) $x = -2, y = -1$ or $x = -0.25, y = 0.125$

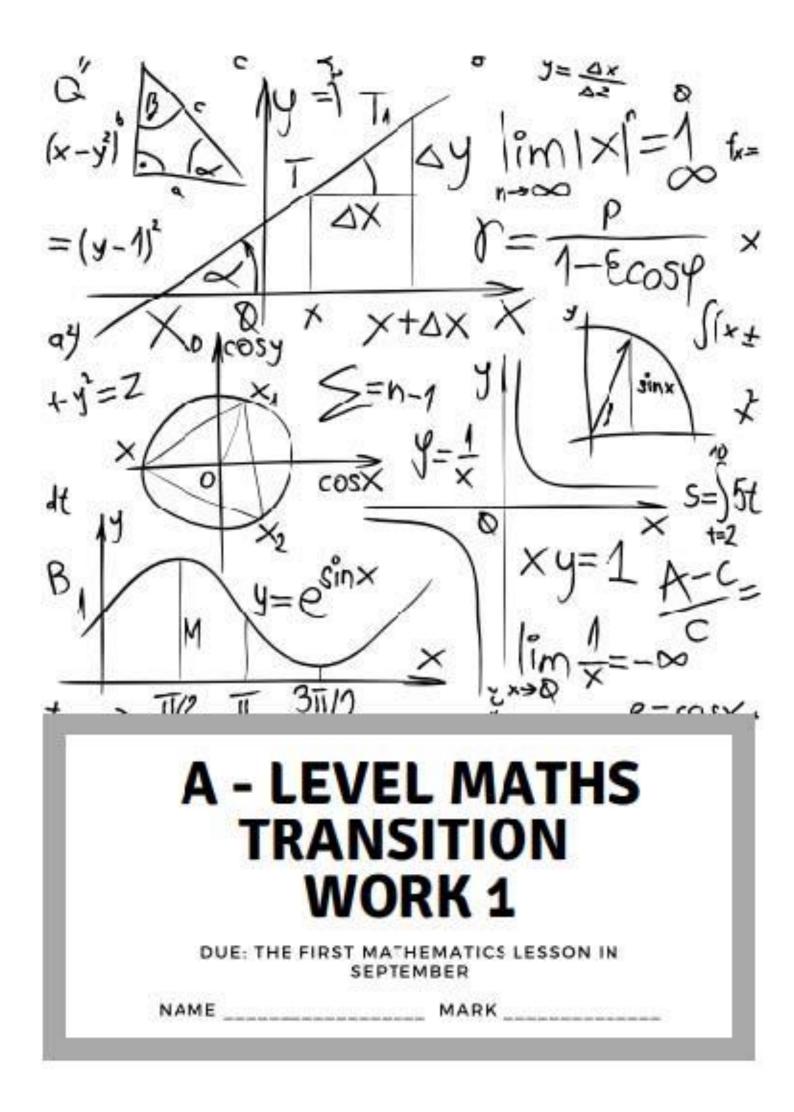
Unit 6 – Answers

Practice Exercise 5.1

1.	a 5.47 cmd 7.79 cm	b 17.1 cme 25.5 cm	11.6 cm 9.18 cm
2.	a 24.2 cm	b 29.6 cm	
3.	a 37.7°d 45.6°	b 46.2°e 47.1°	19.7° 43.6°
4.	 a 13 cm b i 19.8 cm c i 67.4° 	ii 19.2 cm ii 38.7°	
5.	a 15.6 m b i 26.6°	ii 36.9° iii 22.6°	

Practice Exercise 5.2

1.	a 8.06 cm	b 7.19 cm	c 6.35 cm
2.	a 45.0°	b 63.6°	c 23.6°
3.	a 8.79 cm	b 12.6 cm	c 5.01 cm
4.	a 54.7°	b 81.2°	c 46.0°
5.	i 21.9 cm ²	ii 29.2	cm ²
6.	33.3°		
7.	16.8 m ²		
8.	a 6.76 cm	b 75°	c 13.1 cm d 19.9 cm



This section of the Bridging Unit is **compulsory** and **must** be handed in during your first Mathematics lesson.

You are expected to submit this homework in during the first Mathematics lesson after the summer holidays. In the new academic year you will sit a test as part of the transition period. The test will focus on many of the skills included in this booklet. The knowledge and skills assessed in this booklet, and on the induction test, are required for success in A-Level Mathematics. Therefore, it is essential that you are confident in all the skills included in this booklet.

Success in A-Level Mathematics relies on an excellent attitude to learning and commitment to your studies. If you are struggling with any of the content in this book, you must use the video links included to brush up on these key skills. The videos stated are accessible on <u>www.hegartymaths.com</u> (if you have access to this through your current school) OR <u>www.corbettmaths.com</u> (for everyone).

> You are expected to write neatly, show the method clearly. Diagrams should be drawn using a pencil and ruler.

Content

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Completing the Square	11
Inequalities	13

LAWS OF INDICES

Hegarty Maths No: 102-110						
Corbe	Corbett Maths: 173, 174, 176					
1.	(a) Simplify $m^5 \div m^3$					
	(b) Simplify $5x^4y^3 \times x^2$	y				
2.	Write these numbers in Start with the smallest n					
	5-1 0.5	-5	5°			
3.	Write down the value of	$125^{\frac{2}{2}}$				
5.		123°				
-		-0				
4.	(a) Find the value of	5 ⁰				
	(b) Find the value of	27 ^{1/3}				
	. ,					
	(c) Find the value of	2 ⁻³				
5.	(a) Write down the val	ue of $64^{\frac{1}{2}}$				
	(b) Find the value of	$\left(\frac{8}{125}\right)^3$				

SURDS

Hegarty Maths No: 115-119, 500

Corbett Maths: 305 - 308

1. Write
$$\frac{\sqrt{18} + 10}{\sqrt{2}}$$
 in the form $a + b\sqrt{2}$ where *a* and *b* are integers

2. (a) Rationalise the denominator of $\frac{1}{\sqrt{3}}$

(b) Expand $(2+\sqrt{3})(1+\sqrt{3})$ Give your answer in the form $a+b\sqrt{3}$ where *a* and *b* are integers.

.....

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3. Work out $(5 + \sqrt{3})(5 - \sqrt{3})$

$$\frac{(5+\sqrt{3})(5-\sqrt{3})}{\sqrt{22}}$$

Give your answer in its simplest form.

- **3.** (a) Rationalise the denominator of $\frac{1}{\sqrt{7}}$
 - (b) (i) Expand and simplify $(\sqrt{3} + \sqrt{15})^2$ Give your answer in the form $a+b\sqrt{3}$ where *a* and *b* are integers.

(ii) All measurements on the triangle are in centimetres.*ABC* is a right-angled triangle.*k* is a positive integer.

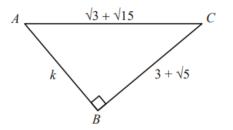


Diagram **NOT** accurately drawn

Find the value of k.

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CHANGING THE SUBJECT FOR A FORMULA

Hegarty Maths No: 280-286

Corbett Maths: 7, 8

1. Make *u* the subject of the formula

 $D = ut + kt^2$

2. Rearrange (q - c) = d to make q the subject.

q =

u =

3. Make *x* the subject of

$$5(x-3) = (4-3x)$$

x =

4. Rearrange the formula to make *a* the subject.

$$P = \frac{n^2 + a}{n + a}$$

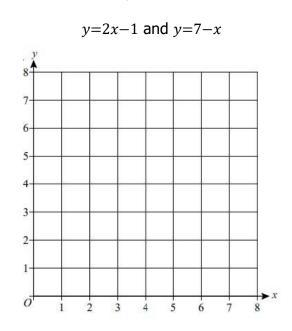
a =.....

SIMULTANEOUS EQUATIONS (LINEAR AND NON-LINEAR)

Hegarty Maths No: 192-194, 218-219, 246, 259

Corbett Maths: 295 - 298

1. Use the axes provided to solve the simultaneous equations.



2. Solve the simultaneous equations

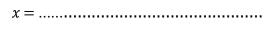
(a)
$$3x + 4y = 5$$

 $2x - 3y = 9$
(b) $2x + 3y = \frac{2}{3}$
 $3x - 4y = 18$



3. Solve the equations

$$x^2 + y^2 = 36$$
$$x = 2y + 6$$



y =

4. Solve the equations

$$x + y = 4$$
$$y = x^2 + 3x - 1$$

$$\begin{aligned} x &= \dots \\ y &= \dots \end{aligned}$$

EXPANDING AND FACTORISING QUADRATIC EXPRESSIONS/EQUATIONS

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Hegarty Maths No: 162-164, 168-169, 223-228, 230-233

Corbett Maths: 118, 119, 119a

- **1.** Expand and simplify (m + 7)(m + 3)
- **2.** (a) Factorise 6 + 9x
 - (b) Factorise $y^2 16$
 - (c) Factorise $2p^2 p 10$
- **3.** (a) Factorise $x^2 + 5x + 4$

(b) Expand and simplify (3x-1)(2x+5)

4. (a) Factorise $x^2 + 7x$

(b) Factorise $y^2 - 10y + 16$

(c) (i) Factorise $2t^2 + 5t + 2$

5. Solve, by factorising, the equation $8x^2 + 2x - 15 = 0$

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USING THE QUADRATIC FORMULA

Hegarty Maths No: 241-242

Corbett Maths: 267

1. Solve $3x^2 + 7x - 13 = 0$ Give your solutions correct to 2 decimal places.

x = or *x* =

2. Solve the equation

 $2x^2 + 6x - 95 = 0$ Give your solutions correct to 3 significant figures.

x = or *x* =

3. Solve this quadratic equation. $x^2 = 5x + 8$ Give your answers correct to 3 significant figures.

x = or *x* =

COMPLETING THE SQUARE

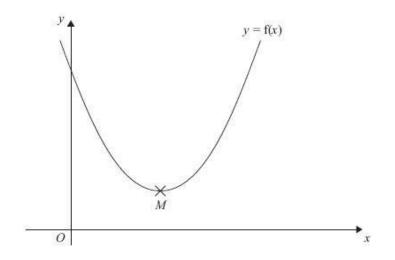
Hegarty Maths No: 235-239

Corbett Maths: 267a, 265

1. The expression $x^2 - 8x + 21$ can be written in the form $(x+a)^2 + b$ for all values of x. (a) Find the value of a and the value of b.

> *a* = *b* =

The equation of a curve is y = (x) where $(x) = x_2 - 8x + 21$ The diagram shows part of a sketch of the graph of y = (x).



The minimum point of the curve is *M*. (b) Write down the coordinates of *M*.

.....

2. Sketch the graph of $(x) = x^2 - 5x + 10$, showing the coordinates of the turning point and the coordinates of any intercepts with the coordinate axes.

3. (a) Write $2x^2 + 16x + 35$ in the form $a(x+b)^2 + c$ where *a*,*b*, and *c* are integers.

.....

(b) Hence, or otherwise, write down the coordinates of the turning point of the graph of $y = 2x^2 + 16x + 35$

.....

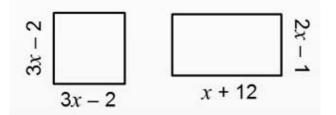
INEQUALTIES

Hegarty Maths No: 270-277

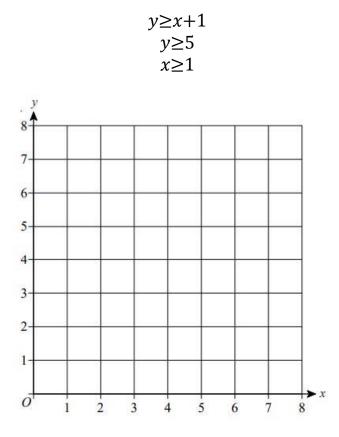
Corbett Maths: 178, 179, 182

- Find the range of values of *x* that is satisfied by the following inequalities below.
 You must show your working out.
 - (1 a) ve $8x 3 \ge 9$ (2 b) ve $5(3x - 2) \le 125$ (3 c) ve $\frac{2x - 3}{5} > 9$ (4 d) ve $\frac{3}{8}(5x + 1) \le 66$ (5 e) ve $-7 \le 5x + 3 \le 23$ (6 f) ve $1 \le 6 - 5x \le 41$

2. For what values of *x* is the perimeter of the square greater than the perimeter of the rectangle?



3. On the axes provided, draw straight lines, and use shading, to show the region R that satisfies the inequalities detailed.



4. On the axes provided, draw straight lines, and use shading, to show the region R that satisfies the inequalities detailed.

